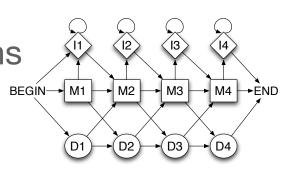
Advanced Database Searching: Sequence Patterns, Profiles & Hidden Markov Models

BI 527, Lecture #14, Fall 2011

VGA--NAGRPY
VG---NVDKPV
VGA--NVAHPH
VAA----PH
VGS--TYEKPS
FGA--NFEKPH
IGAADNGARPY

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Recap of the last lecture: #13

Sequence motifs and patterns

Finding functional cues from sequence conservation

Patterns that describe a motif using a qualitative regular expression sequence

[LFI]-x-G-[PT]-P-G-x-G-K-[TS]-[AGSI]

Defining and using patterns and their limitations

Sequence profiles

Profiles describe a motif using quantitative information captured in a **PSSM**Building log-likelihood ratio PSSMs
The average score method for protein PSSMs
Scoring sequences and searching with profiles

• **PSI-BLAST** algorithm

Iterative PSSM searching to improve BLAST search sensitivity PSSM advantages and limitations
The danger of PSSM corruption (triangular inequality)

Profile software and databases

Outline of this lecture: #14

• Major **PSSM limitations**

Do not capture positional dependencies Hard to recognize pattern instances that contain indels Do not handle boundary detection problems well

Modeling motifs using Markov chains:

Pros and cons of Markov models

Hidden Markov models (HMMs)

More versatile full probabilistic model for detection of remote similarities Architecture and parameterization

Boundary detection

Key algorithms: Viterbi, Forward and Baum-Welch algorithms

Scoring sequences and generating MSAs

HMM limitations

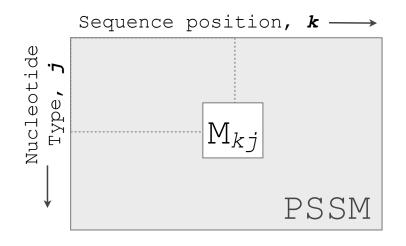
HMM software and databases

Summary and example usage

Position Specific Scoring Matrices

A sequence profile is a **position-specific scoring matrix** (or **PSSM**) that gives a *quantitative* description of a sequence motif.

A simple PSSM is a Log odds scoring matrix that has as many columns as there are positions in the alignment, and either 4 rows (one for each DNA nucleotide) or 20 rows (one for each amino acid).



$$\boldsymbol{M}_{kj} = \log\left(\frac{p_{kj}}{p_j}\right)$$

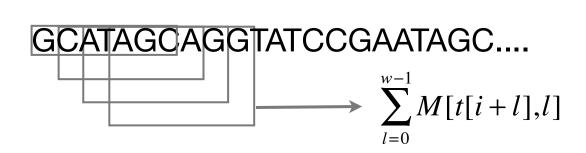
 \mathbf{M}_{kj} score for the *j*th nucleotide at position *k* \mathbf{p}_{kj} probability of nucleotide *j* at position *k* \mathbf{p}_{j} "background" probability of nucleotide *j*

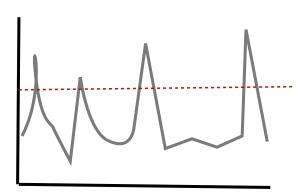
Problems with PSSMs

PSSMs work well for fixed length motifs in which the sites are more or less independent - i.e., ungapped motifs

However there are other kinds of motifs for which PSSMs are not well suited. PSSMs cannot:

- 1. model positional dependencies
- 2. recognize pattern instances containing insertions or deletions
- 3. model variable length patterns
- 4. detect boundaries





Problems with PSSMs: 1. Positional dependencies

Do not capture positional dependencies

WEIRD
WEIRD
WEIQH
WEIRD
WEIRD

D					0.6
Ε		1.0			
Н					0.4
I			1.0		
Q				0.4	
R				0.6	
W	1.0				

Note: We <u>never</u> see **QD** or **RH**, we only see **RD** and **QH**. However, P(RH)=0.24, P(QD)=0.24, while P(QH)=0.16

Problems with PSSMs: 2. Insertions and deletions

Hard to recognize pattern instances that contain indels

D	0.8	0.8	0.8	0.8	2.4
E	0.6	2.9	0.6	0.6	1.6
Н	2.0	2.0	2.0	2.0	3.0
	0.8	0.8	3.1	0.8	0.8
Q	1.1	1.1	1.1	2.1	1.1
R	8.0	8.0	8.0	2.8	8.0
W	5.0	2.7	2.7	2.7	1.8

$$5.0 + 2.9 + 1.2 + 1.4 + 1.5 = 11$$

$$1.2 + 1.8 + 3.1 + 3.0 + 3.4 = 12.5$$



$$5.0 + 2.9 + 3.1 + 3.0 + 3.4 = 18.4$$

Problems with PSSMs: 3. Variable length motifs

Cannot easily deal with variable length motifs

WETIRD

WE-IRD

WETIQH

WE-IRD

WETIQH

Gaps can be represented by expanding Σ but what size window should be used to score new instances of the motif???



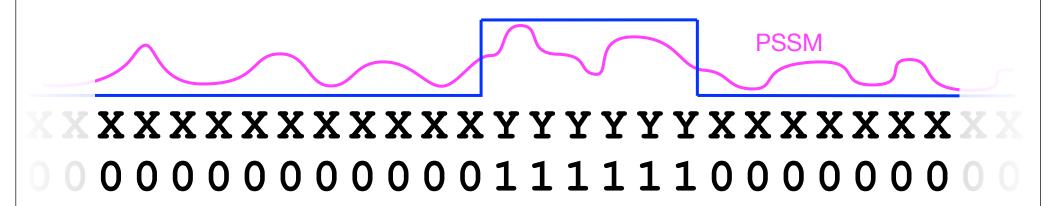
Problems with PSSMs: 4. Detecting boundaries

Do not handle boundary detection problems well

E.g. Label every element in the sequence with a 0 (not in pattern) or a 1 (in pattern)

Examples of boundary detection problems include:

- Recognition of regulatory motifs
- Recognition of protein domains
- Intron/exon boundaries
- Gene boundaries
- Transmembrane regions
- Secondary structure elements (helices and strands)

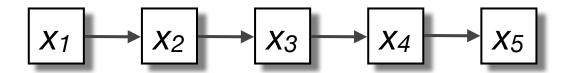


These shortcomings of PSSMs set the stage for a new kind of profile, based on **Markov chains**, called **Hidden Markov models** (**HMMs**)

- modeling positional dependencies
- recognizing pattern instances with indels
- modeling variable length patterns
- detecting boundaries

Markov chains

Markov chains are stochastic processes that undergo **transitions** between a finite series of **states** in a chainlike manner.



The system transverses states with probability

$$p(x_1, x_2, x_3, ...) = p(x_1) p(x_2|x_1) p(x_3|x_2) p(x_4|x_3)...$$

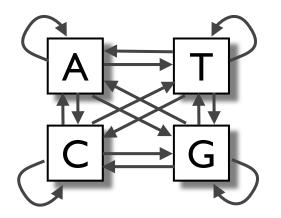
i.e. **Markov chains are memoryless**: the probability that the chain is in state x_i at time t, depends only on the state at the previous time step and not on the past history of the states visited before time t-1.

This specific kind of "memorylessness" is called the **Markov property**.

The **Markov property** states that the conditional probability distribution for the system at the next step (and in fact at all future steps) depends only on the current state of the system, and not additionally on the state of the system at previous steps.

Markov chains...

Markov chains, and their extension hidden Markov models (HMMs), are commonly represented by **state diagrams**, which consist of *states* and connecting *transitions*



E.g., A general Markov chain modeling DNA. Note that any sequence can be traced through the model by passing from one state to the next via the transitions.

A **transition probability** parameter (a_{ij}) is associated with each transition (arrow) and determines the probability of a certain state (S_i) following another state (S_i) .

A Markov chain is defined by:

- a finite set of **states**, S₁, S₂ ... S_N
- a set of *transition probabilities*: $a_{ij} = P(q_{t+1} = S_i | q_t = S_i)$
- and an initial state probability distribution, $\pi_i = P(q_0 = S_i)$

Simple Markov chain example for x={a,b}

Observed sequence: x = abaaababbaa

Model:

transition probabilities

Prev	Next	Prob
i	j	a _{ij}
a	a	0.7
a	b	0.3
b	a	0.5
b	b	0.5

initial state probability distribution

$$\begin{array}{c|c} \textbf{Start} & \textbf{a 0.5} \\ \textbf{probs} & \textbf{b 0.5} \end{array}$$

$$P(x) = 0.5 \times 0.3 \times 0.5 \times 0.7 \times 0.7 \times 0.3 \times 0.5 \times 0.3 \times 0.5 \times 0.5 \times 0.7$$

Q. Can you sketch the state diagram with labeled transitions for this model?

Typical questions we can ask with Markov chains include:

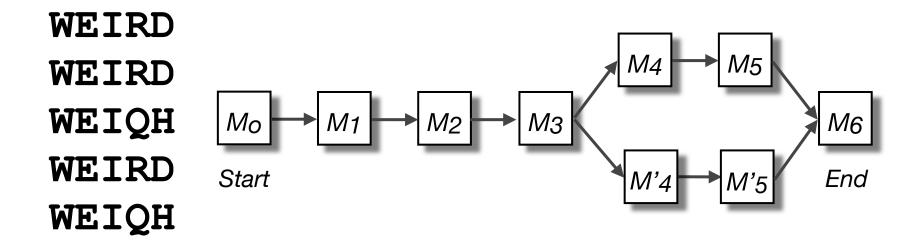
- What is the probability of being in a particular state at a particular time?
 (By time here we can read position in our query sequence)
- What is the probability of seeing a particular sequence of states?
 (I.e., the score for a particular query sequence given the model)

- Q. What do Markov chains add over the traditional PSSM approach? In particular how do Markov chains deal with the following PSSM weaknesses?
 - 1. Positional dependencies
 - 2. Pattern instances containing insertions or deletions
 - 3. Variable length patterns, and
 - 4. The detection boundaries (i.e. segmentation of sequences)

Markov chains: 1. Positional dependencies



The connectivity or **topology** of a Markov chain can easily be designed to capture dependencies and variable length motifs.

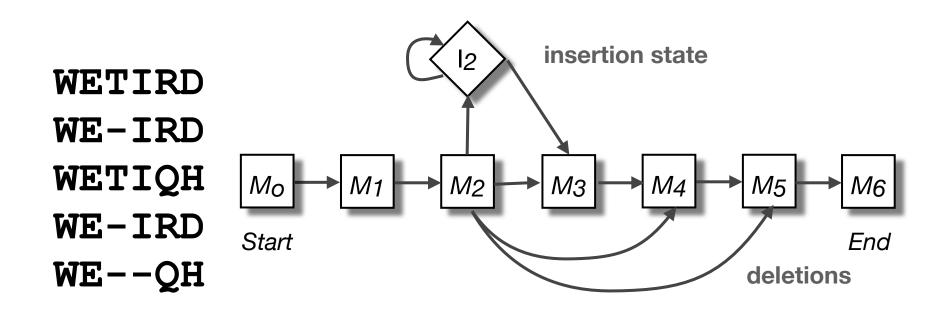


Recall that a PSSM for this motif would give the sequences **WEIRD** and **WEIRH** equally good scores even though the **RH** and **QR** combinations were not observed

Markov chains: 2. Insertions and deletions



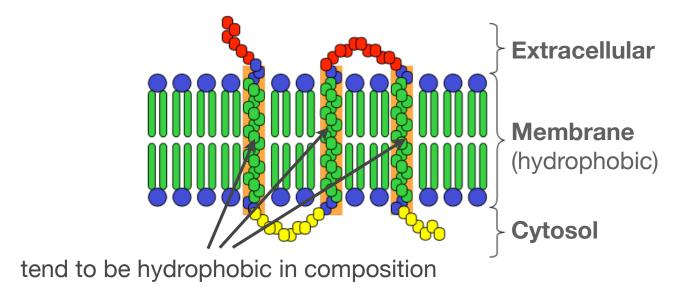
To address pattern instances with gaps and variable length motifs, we can construct a Markov chain to recognize a query sequences with insertions (via an extra insertion state) and deletions (via extra transitions (edges))



Markov chains: 3. Boundary detection



Giving a sequence we wish to label each symbol in the sequence according to its class (e.g. transmembrane regions or extracellular/cytosolic)



Given a training set of labeled sequences we can begin by modeling each amino acid as hydrophobic (**H**) or hydrophilic (**L**)

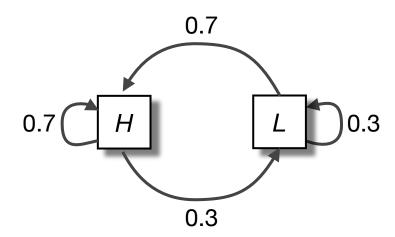
i.e. reduce the dimensionality of the 20 amino acids into two classes

E.g., A peptide sequence can be represented as a sequence of Hs and Ls. e.g. HHHLLHLHLHL...

Markov chains: boundary detection...

A simpler question: is a given sequence a transmembrane sequence?

A Markov chain for recognizing transmembrane sequences



- States: S_H, S_L
- $\Sigma = \{H, L\}$
- $\pi(H) = 0.6$, $\pi(L) = 0.4$

Question: Is sequence **HHLHH** a transmembrane protein?

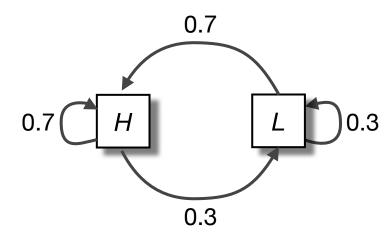
$$P(HHLHH) = 0.6 \times 0.7 \times 0.7 \times 0.3 \times 0.7 \times 0.7 = 0.043$$

Problem: need a threshold, threshold must be length dependent

Markov chains: boundary detection

We can classify an observed sequence $(O = O_1, O_2, ...)$ by its log odds ratio

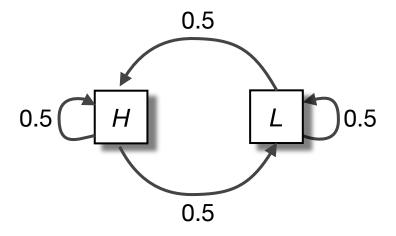
transmembrane model



Transmembrane (TM)

•
$$\pi(H) = 0.6$$
, $\pi(L) = 0.4$

null model



Extracellular/cytosolic (E/C)

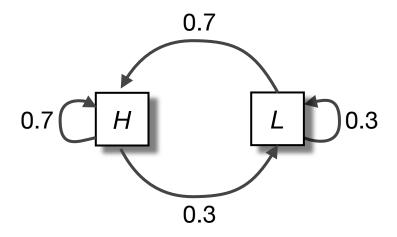
•
$$\pi(H) = 0.5$$
, $\pi(L) = 0.5$

$$\frac{P(HHLHH \mid TM)}{P(HHLHH \mid EC)} = \frac{0.6 \times 0.7 \times 0.7 \times 0.3 \times 0.7 \times 0.7}{0.5 \times 0.5 \times 0.5 \times 0.5 \times 0.5 \times 0.5} = \frac{0.043}{0.016} = 2.69$$

In other words, it is more than twice as likely that **HHLHH** is a transmembrane sequence. The log-odds score is: log₂(2.69) = 1.43

Side note: Parameter estimation

Both initial probabilities ($\pi(i)$)and transition probabilities (a_{ij}) are determined from known examples of transmembrane and non-transmembrane sequences.



- initial probabilities $\pi(H)$, $\pi(L)$
- transition probabilities: a_{HH} , a_{HL} , a_{LH} and a_{LL} .

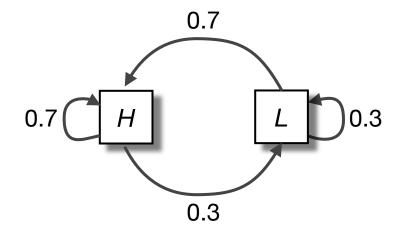
Given labeled sequences (TM and E/C), we determine the initial probabilities $\pi(i)$ by counting the number of sequences that begin with residue i.

To determine transition probabilities, a_{ij} , we first determine A_{ij} (the number of transitions from state i to j in the training data, i.e. count the number of ij pairs in the training data). Then normalize by the number of i^* pairs.

$$a_{ij} = \frac{A_{ij}}{\sum_{i'} A_{ij'}}$$

Side note: Parameter estimation...

Both initial probabilities ($\pi(i)$)and transition probabilities (a_{ij}) are determined from known examples of transmembrane and non-transmembrane sequences.



 $\pi(H)$ = # of sequences that begin with H, normalized by the total # of training sequences

•
$$\pi(H) = 0.6$$
, $\pi(L) = 0.4$

HH... (
$$A_{HL} = 12, A_{H^*} = 40$$
)

$$a_{HL} = \frac{A_{HL}}{\sum_{i} A_{Hi}}$$
 #HL pairs 12

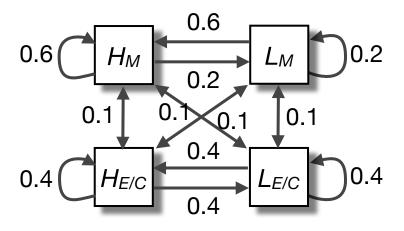
H* pairs 40

Boundary detection challenge

Given sequence of Hs and Ls, find all transmembrane regions:

Using our Markov models we would still need to score successive overlapping windows along the sequence, leading to a fuzzy boundary (just as with a PSSM).

To approach this question we can construct a new four state model by adding transitions connecting the TM and E/C models



Transitions between the *M* states and the *E/C* states indicate boundaries between membrane regions and cytosolic or extracellular regions.

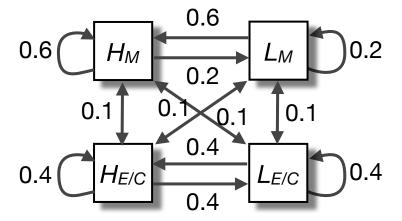
However this is no longer a standard Markov chain!

Boundary detection challenge...

In a Markov chain, there is a one-to-one correspondence between symbols and states, which is not true of our new merged four state, two symbol model.

For example, both H_M and $H_{E/C}$ are associated with hydrophilic residues.

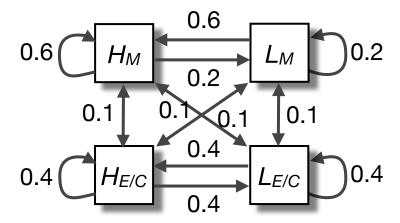
- This four-state transmembrane model is a hidden Markov model.



So whats hidden?

We will distinguish between the *observed* parts of the problem and the *hidden* parts

- In the Markov models we have considered previously it is clear which states account for each part of the observed sequence
 Due to the one-to-one correspondence between symbols and states
- In our new model, there are multiple states that could account for each part of the observed sequence
 - i.e. we don't know which state emitted a given symbol from knowledge of the sequence and the structure of the model
 - ▶ This is the hidden part of the problem

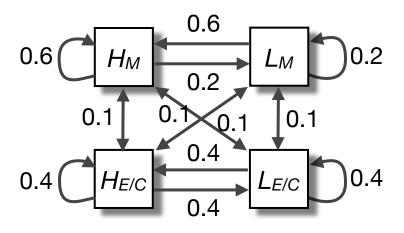


For our Markov models

Given HLLH..., we know the exact state sequence (q₀=S_H, q₁=S_L, q₂=S_L, ...)

For our HMM

- Given HLLH..., we must infer the most probable state sequence
- This HMM state sequence will yield the boundaries between likely TM and E/C regions



```
HM, LM, LM, HM
HM, LM, LM, HE/C
HM, LM, LH/C, HM
HM, LM, LH/C, HE/C
HM, LE/C, LM, HM
HM, LE/C, LM, HE/C
HM, LE/C, LH/C, HM,
HM, LE/C, LH/C, HE/C,
HE/C, LM, LM, HM
HE/C, LM, LM, HE/C
HE/C, LM, LH/C, HM
HE/C, LM, LH/C, HE/C
HE/C, LE/C, LM, HM
HE/C, LE/C, LM, HE/C
HE/C, LE/C, LH/CM, HM
HE/C, LE/C, LH/CM, HE/C
```

Side note: HMM states as sequence emitters

It's useful to imagine HMM states emitting symbols each time they are visited

In this way, transversing the model will "generate" a sequence with a certain probability (i.e. "score").

This probability is a product of the state path taken through the model

That is, it depends on *initial probabilities*, *transition probabilities* and *emission probabilities* (the probability that a visited state emits a particular symbol)

along the path

There may be many possible paths that can generate the same sequence

An HMM is a **full probabilistic model** – the model parameters θ and the overall sequence "scores" $P(x, S \mid HMM, \theta)$ are all probabilities. As a result, we can use standard **Bayesian probability theory** to manipulate these numbers in powerful ways, including optimizing parameters, calculating confidence in predictions, and interpreting the statistical significance of scores.

Hidden Markov models (HMMs)

Markov Chains

- States: *S*₁, *S*₂ ...*S*_N
- Initial probabilities: π_i
- Transition probabilities: aij

One-to-one correspondence between states and symbols

Hidden Markov Models

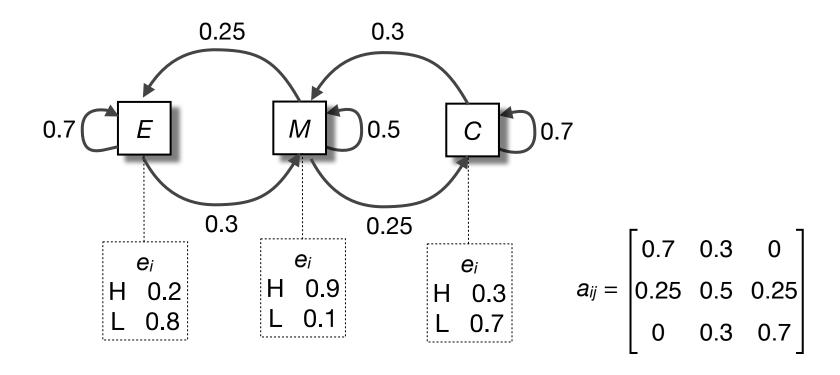
- States: *S*₁, *S*₂ ...*S*_N
- Initial probabilities: π_i
- Transition probabilities: aii
- Alphabet of emitted symbols, Σ
- Emission probabilities: e_i(a)
 probability state i emits symbol a

Symbol may be emitted by more than one state

Similarly, a state can emit more than one symbol

Example three state HMM

In this example we will use only one state for the transmembrane segment (M) and use emission probabilities to distinguish between H and L residues. We will also add separate E & C states with distinct emission probabilities.

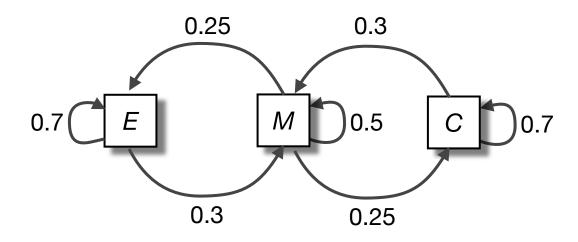


Side note: Parameter estimation

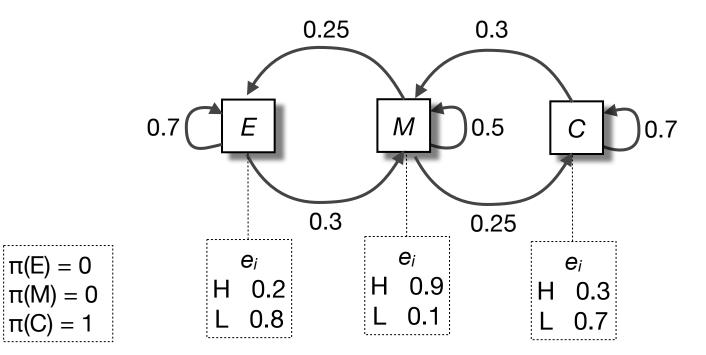
As in the case of Markov chains, the HMM parameters can be learned from labeled training data

Note that we now have to learn the initial probabilities, transition probabilities and *emission probabilities*

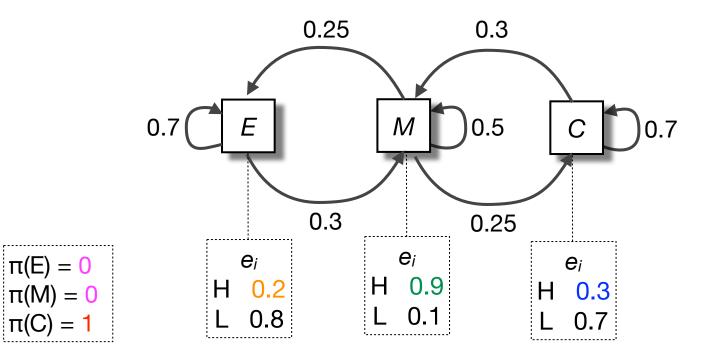
$$a_{ij} = \frac{A_{ij}}{\sum_{j'} A_{ij'}}$$
 $e_i(x) = \frac{E_i(x)}{\sum_{x} E_i(x')}$



	Ε	М	С
π_i	0	0	1
e _i (H)	0.2	0.9	0.3
e _i (L)	0.8	0.1	0.7



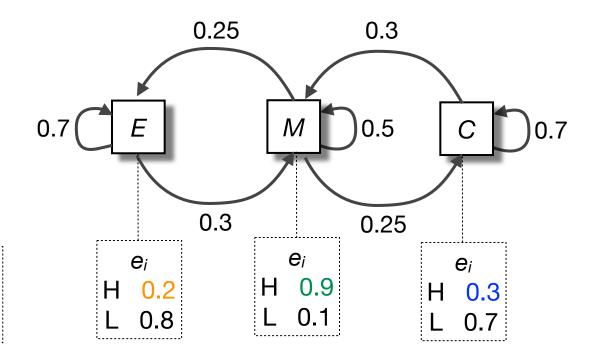
States	Н	Н	L	L	Н
E					
М					
С					



States	H	H	L	L	Н
Ε	0x0.2 =0				
М	0x0.9 =0				
С	1×0.3 =0.3				

START

 $\pi(C) = 1$

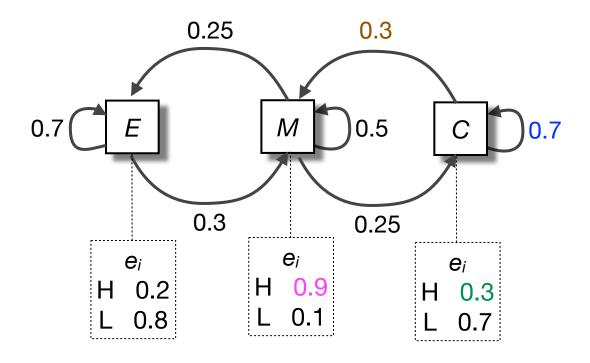


States	H	H	L	L	H
Ε	0x0.2 =0				
М	0x0.9 =0				
C	1x0.3 =0.3				

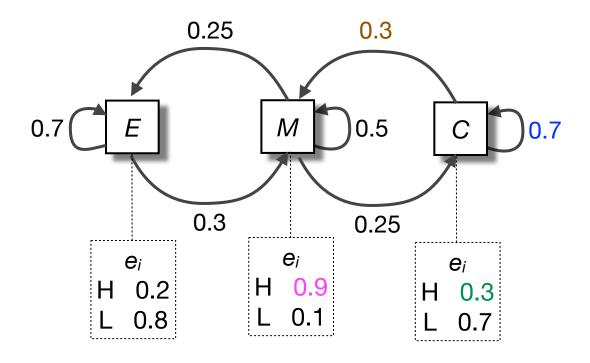
START

 $\pi(E) = 0$ $\pi(M) = 0$

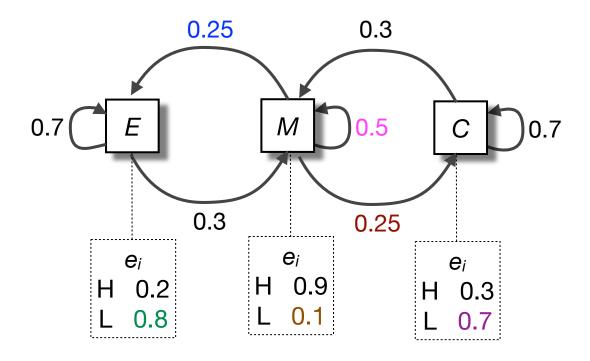
 $\pi(C) = 1$



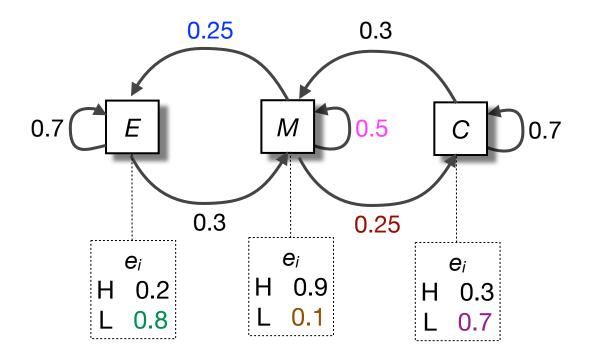
States	H	Н	L	L	Н
Ε	0×0.2 =0	-			
М	0×0.9 =0	0.3×0.9×0.3 =0.081			
C	1x0.3 =0.3	0.7×0.3× <mark>0.3</mark> =0.063			



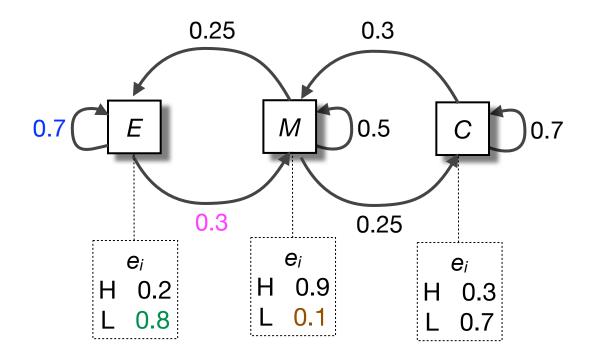
States	Н	H	L	L	H
Ε	0×0.2 =0	-			
М	0×0.9 =0	0.3x0.9x0.3 =0.081			
С	1x0.3 =0.3	0.7×0.3× <mark>0.3</mark> =0.063			



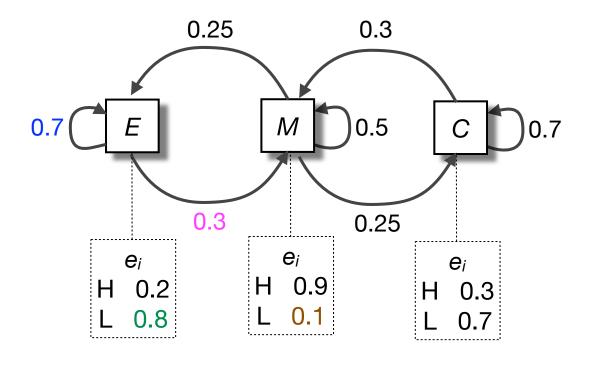
States	H	Н	L	L	H
Ε	0×0.2 =0	-	0.25×0.8×0.081 =0.016		
М	0×0.9 =0	0.3×0.9×0.3 =0.081	0.5×0.1×0.081 =0.04		
C	1×0.3 =0.3	0.7×0.3.0.3 =0.063	0.25×0.7×0.081 =0.014		



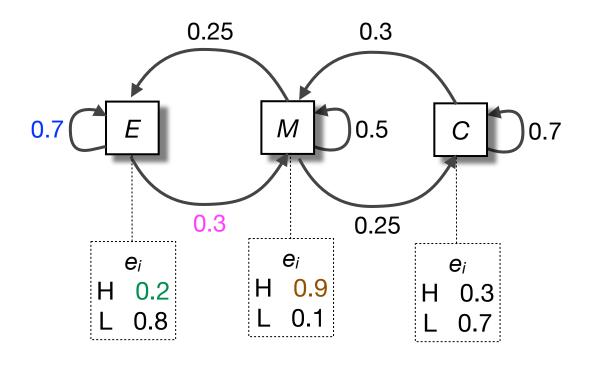
States	H	H	L	L	H
Ε	0×0.2 =0	-	0.25×0.8×0.081 =0.016		
М	0×0.9 =0	0.3×0.9×0.3 =0.081	0.5×0.1×0.081 =0.04		
C	1×0.3 =0.3	0.7×0.3.0.3 =0.063	0.25×0.7×0.081 =0.014		



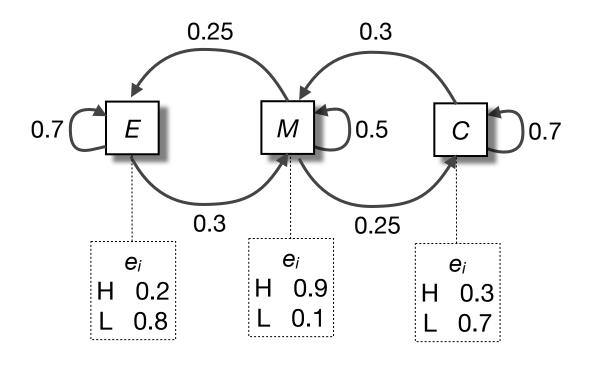
States	H	Н	L	L	Н
Ε	0×0.2 =0	-	0.25×0.8×0.081 =0.016	0.7×0.8×0.016 =0.009	
М	0×0.9 =0	0.3×0.9×0.3 =0.081	0.5×0.1×0.081 =0.04	0.3×0.1×0.016 =0.0005	
C	1x0.3 =0.3	0.7×0.3.0.3 =0.063	0.25×0.7×0.081 =0.014	-	



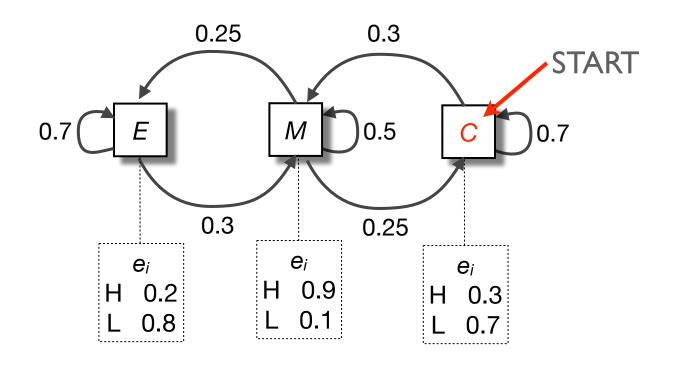
States	Н	H	L	L	H
Ε	0×0.2 =0	1	0.25×0.8×0.081 =0.016	$0.7 \times 0.8 \times 0.016$ = 0.009	
М	0x0.9 =0	0.3×0.9×0.3 =0.081	0.5×0.1×0.081 =0.04	0.3×0.1×0.016 =0.0005	
C	1x0.3 =0.3	0.7×0.3.0.3 =0.063	0.25×0.7×0.081 =0.014	-	



States	Н	Н	L	L	Н
Ε	0×0.2 =0	1	0.25×0.8×0.081 =0.016	0.7×0.8×0.016 =0.009	0.7x0.2x0.009 =0.001
М	0×0.9 =0	0.3×0.9×0.3 =0.081	0.5×0.1×0.081 =0.04	0.3×0.1×0.016 =0.0005	0.3×0.9×0.009 =0.002
C	1x0.3 =0.3	0.7×0.3.0.3 =0.063	0.25×0.7×0.081 =0.014	-	-



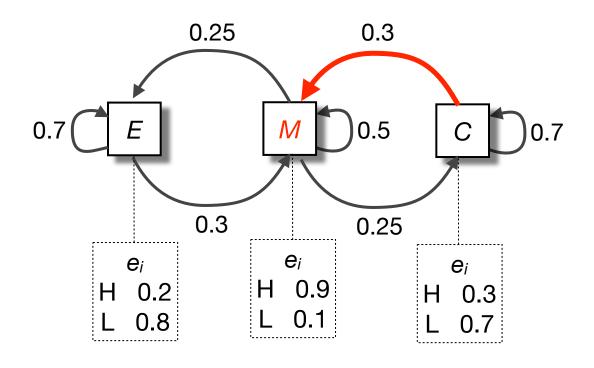
States	H	Н	L	L	Н
Ε	0×0.2 =0	-	0.25×0.8×0.081 =0.016	0.7×0.8×0.016 =0.009	0.7×0.2×0.009 =0.001
М	0×0.9 =0	0.3×0.9×0.3 =0.081	0.5×0.1×0.081 =0.04	0.3×0.1×0.016 =0.0005	0.3×0.9×0.009 =0.002
C	1x0.3 =0.3	0.7×0.3.0.3 =0.063	0.25×0.7×0.081 =0.014	-	-



States	Н	Н	L	L	Н
Ε	0×0.2 =0	-	0.25×0.8×0.081 =0.016	0.7×0.8×0.016 =0.009	0.7×0.2×0.009 =0.001
М	0×0.9 =0	0.3×0.9×0.3 =0.081	0.5×0.1×0.081 =0.04	0.3×0.1×0.016 =0.0005	0.3×0.9×0.009 =0.002
С	1x0.3 =0.3	0.7×0.3.0.3 =0.063	0.25×0.7×0.081 =0.014	-	-

START

C

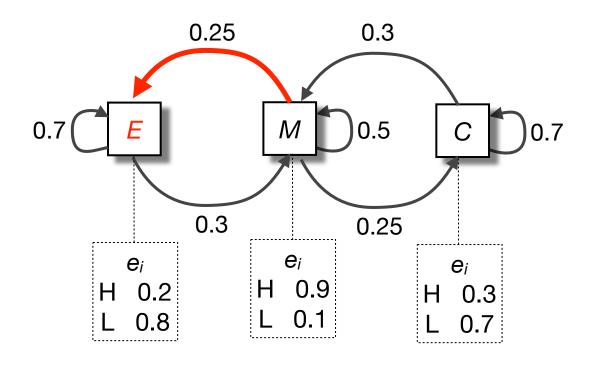


States	Н	Н	L	L	H
Ε	0×0.2 =0	-	0.25×0.8×0.081 =0.016	0.7×0.8×0.016 =0.009	0.7×0.2×0.009 =0.001
М	0x0.9 =0	0.3×0.9×0.3 =0.081	0.5×0.1×0.081 =0.04	0.3×0.1×0.016 =0.0005	0.3×0.9×0.009 =0.002
C	1x0.3 =0.3	0.7×0.3.0.3 =0.063	0.25×0.7×0.081 =0.014	-	-

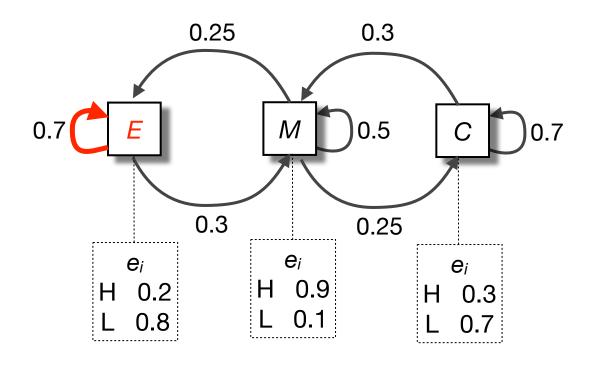
START |

C

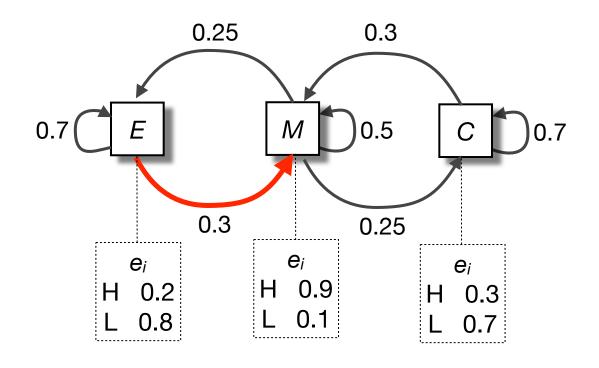
M



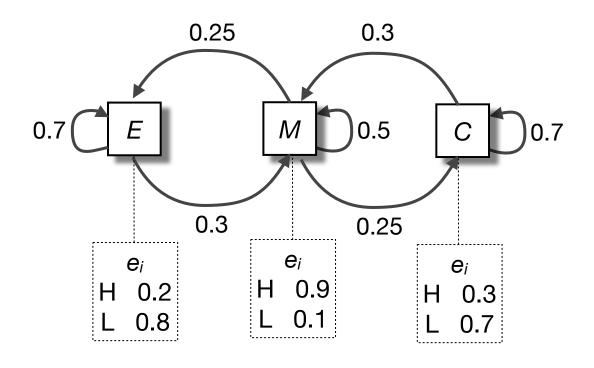
States	Н	Н	L	L	Н
E	0×0.2 =0	-	0.25×0.8×0.081 =0.016	0.7×0.8×0.016 =0.009	0.7×0.2×0.009 =0.001
М	0×0.9 =0	0.3×0.9×0.3 =0.081	0.5×0.1×0.081 =0.04	0.3×0.1×0.016 =0.0005	0.3×0.9×0.009 =0.002
C	1x0.3 =0.3	0.7×0.3.0.3 =0.063	0.25×0.7×0.081 =0.014	-	-
START	С	М	E		



States	Н	Н	L	L	Н
Ε	0×0.2 =0	1	0.25×0.8×0.081 =0.016	0.7×0.8×0.016 =0.009	0.7×0.2×0.009 =0.001
М	0×0.9 =0	0.3×0.9×0.3 =0.081	0.5×0.1×0.081 =0.04	0.3×0.1×0.016 =0.0005	0.3×0.9×0.009 =0.002
C	1x0.3 =0.3	0.7×0.3.0.3 =0.063	0.25×0.7×0.081 =0.014	-	-
START	С	М	E	E	



States	Н	Н	L	L	Н
Ε	0×0.2 =0	1	0.25×0.8×0.081 =0.016	0.7×0.8×0.016 =0.009	0.7×0.2×0.009 =0.001
М	0×0.9 =0	0.3×0.9×0.3 =0.081	0.5×0.1×0.081 =0.04	0.3×0.1×0.016 =0.0005	0.3×0.9×0.009 =0.002
C	1x0.3 =0.3	0.7×0.3.0.3 =0.063	0.25×0.7×0.081 =0.014	-	-
START	С	М	E	E	М



States	Н	Н	L	L	Н
Ε	0×0.2 =0	-	0.25×0.8×0.081 =0.016	0.7×0.8×0.016 =0.009	0.7×0.2×0.009 =0.001
М	0×0.9 =0	0.3×0.9×0.3 =0.081	0.5×0.1×0.081 =0.04	0.3×0.1×0.016 =0.0005	0.3×0.9×0.009 =0.002
С	1×0.3 =0.3	0.7×0.3.0.3 =0.063	0.25×0.7×0.081 =0.014	-	-

START

C

M

Ε

Е

M

Most Probable State Sequence

We have just used the Viterbi algorithm

The **Viterbi algorithm** finds the most probable "state path" (S^*) (i.e. sequence of hidden states) for generating a given sequence ($x = x_1, x_2,...x_N$)

$$S^* = argmax P(x,S)$$

This process is often called **decoding** because we "decode" the sequence of symbols to determine the hidden sequence of states

HMMs were original developed in the field of speech recognition, where speech is "decoded" into words or phonemes to determine the meaning of the utterance

Note that we could have used brute force by calculating P(x|S) for all paths but this quickly becomes intractable for longer sequences or HMMs with a large number of states

The Viterbi algorithm is guaranteed to find the most probable state path given a sequence and an HMM

See Durbin et al. Biological Sequence Analysis

Three key HMM algorithms

Viterbi algorithm

Given observed sequence x and an HMM M, composed of states S, calculate the most likely state sequence, S^*

$$S^* = argmax P(x,S)$$

Forward algorithm

Given observed sequence x and an HMM composed of states S, calculate the probability of the sequence for the HMM, P(x|M)

$$P(x) = \sum_{S} P(x,S)$$

Baum-Welch algorithm

Given many observed sequences, estimate the parameters of the HMM

▶ heuristic expectation maximization method to optimize of *a_{ij}* and *e_i(a)*

The forward algorithm

Another important question is how well does a given sequence fit the HMM?

To answer this question we must sum over all possible state paths that are consistent with the sequence in question

(Because we don't know which path emitted the sequence)

The number of paths can quickly become intractable. The **forward algorithm** is a simple dynamic programing solution that makes use of the Markov property so that we don't have to explicitly enumerate every path.

The **forward algorithm** basically replaces the maximization step of the Viterbi algorithm with sums to calculate the probability of the sequence given a HMM.

$$P(x) = \sum_{S} P(x,S)$$

See Durbin et al. Biological Sequence Analysis

The Baum-Welch algorithm

The **Baum-Welch algorithm** is an **heuristic optimization** algorithm for learning probabilistic models in problems that involve hidden states

If we <u>know</u> the state path for each training sequence (i.e. no hidden states with respect to the training sequences), then learning the model parameters is simple (just like it was for Markov chain models)

- count how often each transition and emission occurs
- normalize to get probabilities

If we <u>don't know</u> the path for each training sequence, we can use the **Baum-Welch algorithm**, an expectation maximization method, which estimates counts by considering every path weighted by its probability

- start from a given initial guess for the parameters
- perform a calculation which is guaranteed to improve the previous guess
- run until there is little change in parameters between iterations

For sequence profile-HMMs we train from a MSA and hence we can *estimate* our probabilities from the observed sequences

Segmentation/boundary detection

Given: A test sequence and a HMM with different sequence classes

Task: Segment the sequence into subsequences, predicting the class of

each subsequence

Question: What is the most probable "path" (sequence of hidden states) for

generating a given sequence from the HMM?

Solution: Use the Viterbi algorithm

Classification/sequence scoring

Given: A test sequence and a set of HMMs representing different

sequence classes

Task: Determine which HMM/class best explains the sequence

Question: How likely is a given sequence given a HMM?

Solution: Use the Forward algorithm

Learning/parameterization

Given: A model, a set of training sequences

Task: Find model parameters that explain the training sequences

Question: Can we find a high probability model for sequence characterization

Solution: Use the Forward backward algorithm

Segmentation/boundary detection

Question: What is the most probable "path" (sequence of hidden states) for

generating a given sequence from the HMM?

HMMER: hmmalign - align sequences to our HMM

Classification/sequence scoring

Question: How likely is a given sequence given a HMM?

HMMER: hmmsearch - find sequences that match our HMM

Learning/parameterisation

Question: Can we find a high probability model for sequence characterization

HMMER: hmmbuild - setup our HMM parameters

Half time break...

Questions:

For what kinds of motifs are PSSMs not well suited?

What is the Markov property?

In what important ways do HMMs differ Markov chains?

What is the Viterbi algorithm used for?

How does the Forward algorithm differ from the Viterbi algorithm?

For what kinds of motifs are PSSMs not well suited?

PSSMs are not well suited to pattern instances containing insertions or deletions, variable length patterns and those with positional dependencies.

What is the Markov property?

The Markov property states that the conditional probability distribution for the system at the next step (and in fact at all future steps) depends <u>only</u> on the current state of the system, and not additionally on the state of the system at previous steps.

In what important ways do HMMs differ Markov chains?

HMMs differ from Markov chains in a number of ways:

- In HMMs, the sequence of states visited is hidden. Unlike Markov Chains, there is no longer a one-to-one correspondence between states and output symbols.
- In a HMM the same symbol may be emitted by more than one state.
- In a HMM a state can emit more than one symbol.

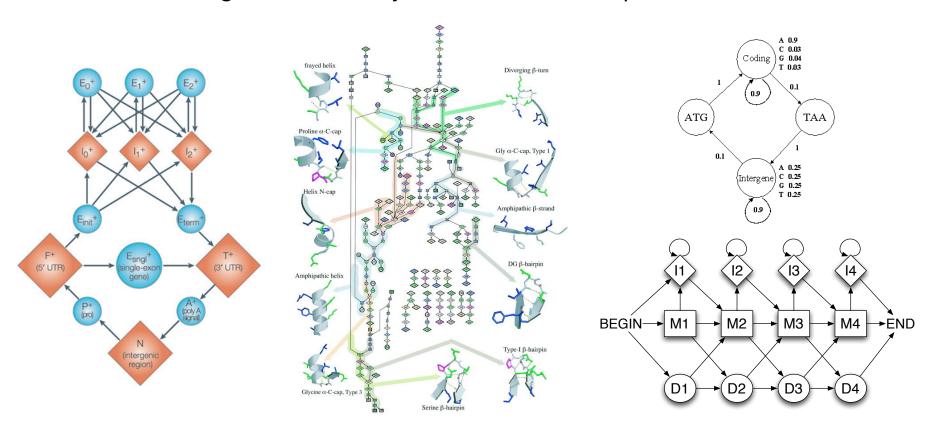
What is the Viterbi algorithm used for?

The Viterbi algorithm is used to find the most probable state path given a sequence and an HMM

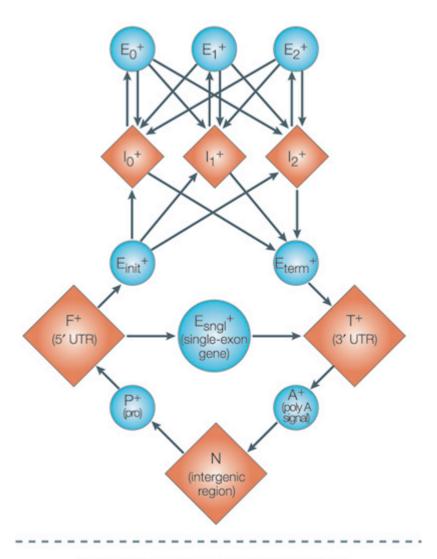
HMM network structure is hand tailored to the problem

No algorithm for the prediction of optimal HMM network structure and probabilities has yet been able to beat simple hand-built topologies

These topologies are tailored to the problem at hand - exon/intron detection, transmembrane regions, secondary structure elements, protein families...



GenScan - gene-prediction HMM

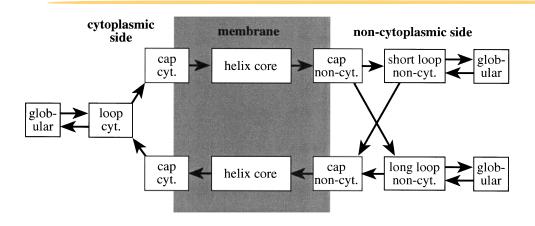


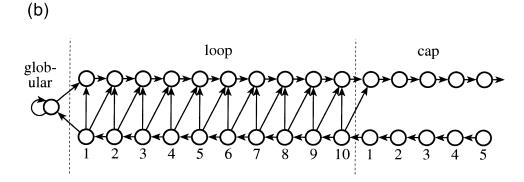
Reverse strand: mirror reflection of above

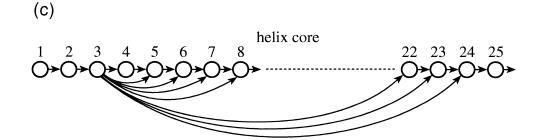
Here, each circle or square represents a functional unit (a state) of a gene on its forward strand (for example, E_{init} is the 5' coding sequence (CDS) and E_{term} is the 3' CDS, and the arrows represent the transition probability from one state to another. The GenScan HMM is trained by pre-computing the transition probabilities from a set of known gene structures.

See: Zhang et al. (2002) Nature Reviews Genetics 3, 698-709

TMHMM - transmembrane protein topology prediction



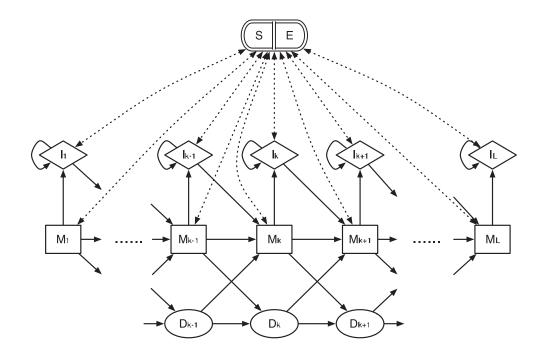




Each box corresponds to one or more states in the HMM. Cyt. represents the cytoplasmic side of the membrane and non-cyt. the other side. (b) The detailed structure of the inside and outside loop models and helix cap models. (c) The structure of the model for the helix core modeling lengths between 5 and 25, which translates to helices between 15 and 35 when the caps are included.

See: Krogh et al. (2001) JMB 305, 567-580

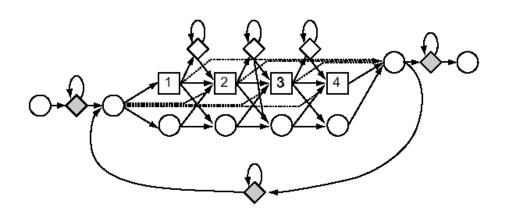
SAMTOOLS - SNP calling in NextGen sequencing data



Application of HMMs in the area of SNP discovery from NextGen sequencing data, to greatly reduce false SNP calls caused by misalignments around insertions and deletions (indels). The central concept is per-Base Alignment Quality, which accurately measures the probability of a read base being wrongly aligned.

See: Li et al. (2011) Bioinformatics 27, 1157–1158

HMMER - protein homology detection and alignment



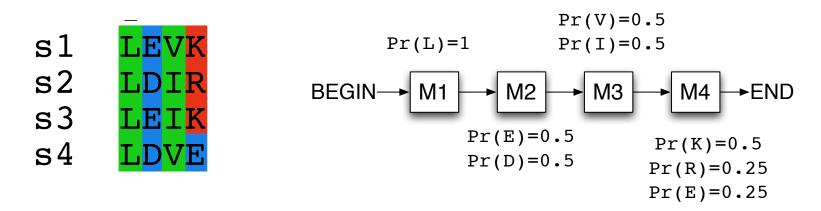
Profile HMM architecture used in HMMER2, SAM and PFTOOLS protein homology detection and alignment packages. *Match states* carry position-specific emission probabilities for scoring residues at each consensus position. *Insert states* emit residues with emission probabilities identical to a background distribution. We will describe this in more detail shortly...

See: Eddy (1998) Bioinformatics 14, 755–763

Building sequence profile-HMMs: Match states

How do the above HMMs relate to profiles? Let's see how we can use the HMM framework to build **profile HMMs** that describe families of related sequences.

In the last lecture, we built a profile for the alignment:

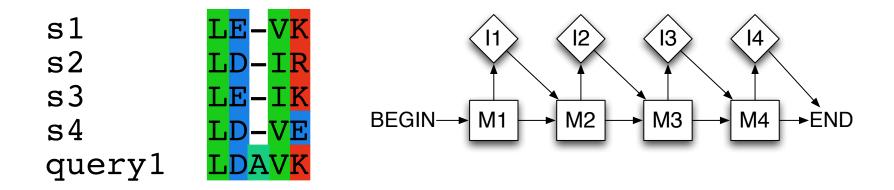


Ignoring the "background" frequencies for now, a profile for this alignment can be viewed as a simple HMM with one "match" state for each column, where consecutive match states are separated by transitions of probability 1.

Q. Why is this not a Markov chain?

Building profile-HMMs: Insert states

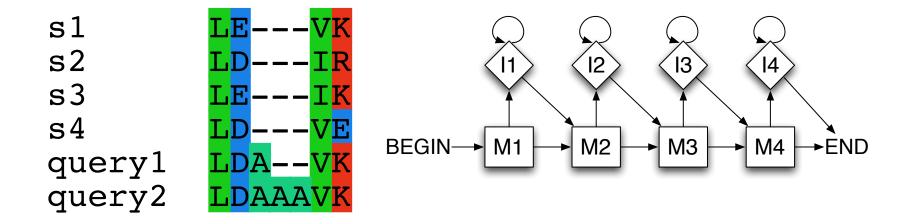
Introduce **insert states** (*Ij*), which will model inserts after the jth column in our alignment.



Typically, the output probabilities for insert states are set equal to the background probabilities. Note that we can have different probabilities for entering different insert states, and this models the fact that insertions may be less well-tolerated in certain portions of the alignment.

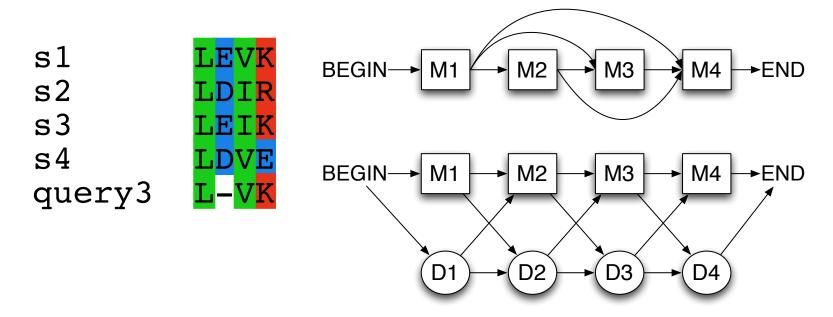
Building profile-HMMs: Insert states + affine gaps

For any particular insert state, we may have different transition probabilities for entering it for the first time *vs.* staying in the insert state; this models *affine* gap penalties.



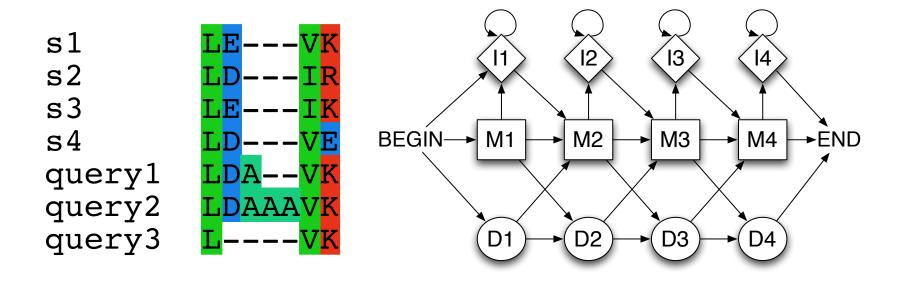
Building profile-HMMs: Delete states

One could model deletions with additional transitions between match states. However, arbitrarily long gaps would introduce lots of transitions in the model. Instead, we will introduce **delete states** that do not emit any symbols



Building profile-HMMs

Putting it all together we get a complete profile HMM topology with match, insert and delete states.



However we still need to decide how many states our HMM has, what the transition probabilities are, etc.

Example profile-HMM building

How do we pick the length of the HMM?
 Common heuristic is to include only those columns that have > 50% occupancy

 How do we pick emission probabilities for match states?

$$b_{m1}(V) = 5/7$$

 $b_{m1}(F) = 1/7$
 $b_{m1}(I) = 1/7$

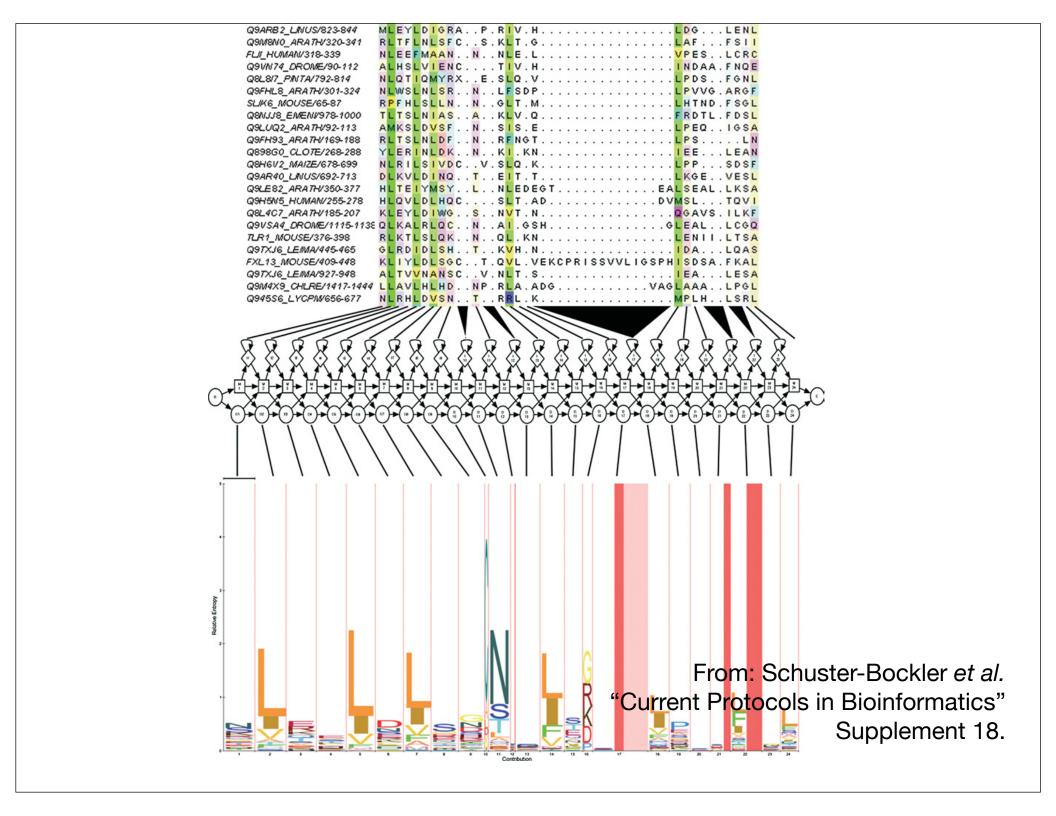
```
S1 VGA--NAGRPY
S2 VG---NVDKPV
S3 VGA--NVAHPH
S4 VAA----PH
S5 VGS--TYEKPS
S6 FGA--NFEKPH
S7 IGAADNGARPY
```

How do we pick transition probabilities?

We let the transition probability of going from state i to state j, aij be equal to:

No. of transitions from state i to state jNo. of transitions from state i to any other state

$$a_{M2M3}(V) = 6/7$$
 No. of matches (=6)
 $a_{M2D3}(F) = 1/7$ No. of gaps (=1)
 $a_{M2I2}(I) = 0/7$ No. of insertions (=0)



Side note: Weighting the training sequences

If there is a high degree of **redundancy** in our initial MSA (i.e. it contains a large group of very closely related sequences and a small number of more distantly related sequences) the resulting HMM will over represent the similar sequences and adversely effect our ability to detect distantly related sequences when searching databases

Sequences weighting attempts to compensate for this *sequence sampling bias* by differentially weighting sequences to reduce redundancy prior to model building

By default HMMER uses a sequence clustering tree as a guide to weight each sequence by its distance to other sequences. This approach will effectively downweight the influence of redundant sequences.

A number of other approaches have been developed (Voronoi algorithm, maximum entropy, etc.)

See: Karchin et al. (1998) Bioinformatics 14, 772-778

Side note: Pseudocounts and Dirichlet distributions

Unfortunately, for alignments containing a small number of sequences the observed counts may not be representative of the family as a whole.

In such cases we must adjust the probabilities to account for our under-sampling (i.e. unobserved residues)

One common approach is to add **pseudocounts** to the observed counts so that no zero probabilities can occur.

Simplest approach is to just add one to all counts. More accurate adjustments consider prior knowledge about the behavior of sequence families adjusting counts according to pre-tabulated **Dirichlet distributions** - which are rather like protein comparison matrixes used in profile methods

Such information is often called **prior information**, indicating that it is known before any sequence data is seen

See: Durbin et al. "Biological Sequence Analysis"

Generating multiple sequence alignments

Large MSAs can be generated very quickly by using the Viterbi algorithm to find the most likely path through the HMM for a set of unaligned sequences

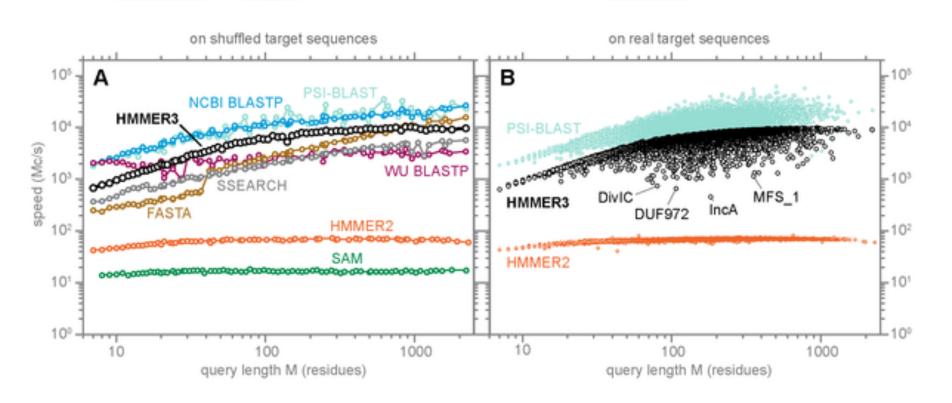
This is the basis of the PFAM database which uses the HMMER software package Namely, HAMMER's *hmmalign* from the results of *hmmsearch*

MSA produced by HMMs are not true MSAs in the way that those produced by ClustalW are. ClustalW compares every sequence to every other sequence, whereas HMM aligning compares every sequence to the model independently so that the alignment between sequences is by proxy. Adding new sequences to the ClustalW alignment will add new information which may alter the alignment of existing sequences; adding new sequences to the HMM alignment never changes the alignment of any sequences relative to each other.

As an alternative to HMMER, you can use the Sequence Alignment and Modeling Software System (SAM)

http://compbio.soe.ucsc.edu/sam.html

HMM sequence searching performance

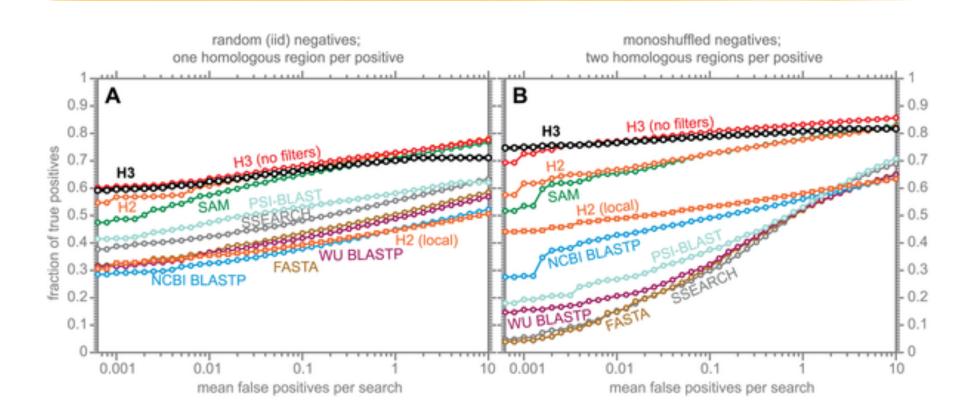


Recent speed benchmarks indicate that HMMER3 is approaching BLAST speed

Each point represents a speed measurement for one search with one query against target sequences. Both axes are logarithmic, for speed in millions of dynamic programming cells per second (Mc/s) on the y-axis and query length on the x-axis.

See: Eddy (2011) PLoS Comp Biol 7(10): e1002195

HMM sequence searching performance...



However HMMER3 has a much higher search sensitivity and specificity

In each benchmark, true positive subsequences have been selected to be no more than 25% identical to any sequence in the query alignment ... (see paper for details).

See: Eddy (2011) PLoS Comp Biol 7(10): e1002195

HMM limitations

HMMs are linear models and are thus **unable to capture higher order correlations** among positions (e.g. distant cysteins in a disulfide bridge, RNA secondary structure pairs, etc).

Another flaw of HMMs lies at the very heart of the mathematical theory behind these models. Namely, that the probability of a sequence can be found from the product of the probabilities of its individual residues.

This claim is only valid if the probability of a residue is independent of the probabilities of its neighbors. In biology, there are frequently **strong dependencies between these probabilities** (e.g. hydrophobic residues clustering at the core of protein domains).

These biological realities have motivated research into new kinds of statistical models. These include hybrids of HMMs and neural nets, dynamic Bayesian nets, factorial HMMs, Boltzmann trees and stochastic context-free grammars.

See: Durbin et al. "Biological Sequence Analysis"

PFAM: Protein Family Database of Profile HMMs

Comprehensive compilation of both multiple sequence alignments and profile HMMs of protein families.

http://pfam.sanger.ac.uk/

PFAM consists of two databases:

- Pfam-A is a manually curated collection of protein families in the form of multiple sequence alignments and profile HMMs. HMMER software is used to perform searches.
- **Pfam-B** contains additional protein sequences that are automatically aligned. Pfam-B serves as a useful supplement that makes the database more comprehensive.
- Pfam-A also contains higher-level groupings of related families, known as clans



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Pfam 25.0 (March 2011, 12273 families)

The Pfam database is a large collection of protein families, each represented by **multiple sequence** alignments and hidden Markov models (HMMs). More...

QUICK LINKS YOU CAN FIND DATA IN PFAM IN VARIOUS WAYS... SEQUENCE SEARCH Analyze your protein sequence for Pfam matches VIEW A PFAM FAMILY View Pfam family annotation and alignments VIEW A CLAN See groups of related families VIEW A SEQUENCE Look at the domain organisation of a protein sequence Find the domains on a PDB structure VIEW A STRUCTURE KEYWORD SEARCH Query Pfam by keywords JUMP TO enter any accession or ID Go Example Enter any type of accession or ID to jump to the page for a Pfam family or clan, UniProt sequence, PDB structure, etc.

Or view the help pages for more information

Citing Pfam

If you find Pfam useful, please consider <u>citing</u> the reference that describes this work:

The Pfam protein families database 2: R.D. Finn, J. Mistry, J. Tate, P. Coggill, A. Heger, J.E. Pollington, O.L. Gavin, P. Gunesekaran, G. Ceric, K. Forslund, L. Holm, E.L. Sonnhammer, S.R. Eddy, A. Bateman

Nucleic Acids Research (2010) Database Issue 38:D211-222

Mirrors

The following are official Pfam mirror sites:

WTSI, UK
 BBC, Sweden
 JFRC, USA

Pfam: Family: Kinesin (PF00225)

Q+ Google







BROWSE SEARCH |

Family: Kinesin (PF00225)



Summary

Domain organisation

Clans

Alignments

HMM logo

Trees

Curation & models

Species

Interactions

Structures

Jump to...

enter ID/acc



Summary

Pfam includes annotations and additional family information from a range of different sources. These sources can be accessed via the tabs below.

Wikipedia: Kinesin

Pfam

Interpro

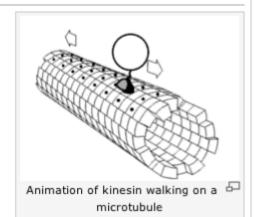
The Pfam group coordinates the annotation of Pfam families in Wikipedia 2. This family is described by a Wikipedia entry entitled "Kinesin 다". More...

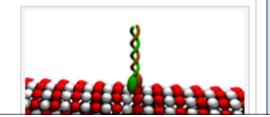
Kinesin Edit Wikipedia article

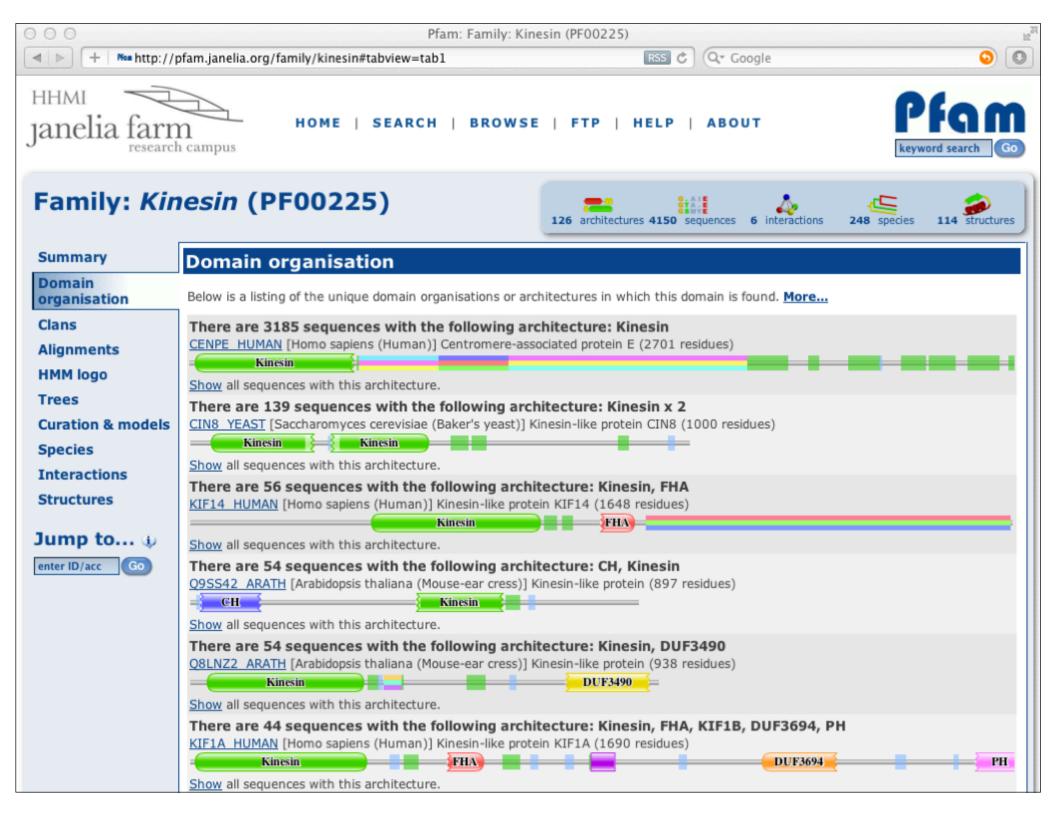
A kinesin is a protein belonging to a class of motor proteins found in eukaryotic cells. Kinesins move along microtubule filaments, and are powered by the hydrolysis of ATP (thus kinesins are ATPases). The active movement of kinesins supports several cellular functions including mitosis, meiosis and transport of cellular cargo, such as in axonal transport. Most kinesins walk towards the plus end of a microtubule, which, in most cells, entails transporting cargo from the centre of the cell towards the periphery. This form of transport is known as anterograde transport.

Contents [show]

- 1 Structure
 - 1.1 Overall structure
 - 1.2 Kinesin motor domain
- 2 Cargo transport
- 3 Direction of motion
- 4 Proposed mechanisms of movement
- 5 Theoretical Modeling of Kinesin
- 6 Kinesin and mitosis
- 7 Family members
- 8 See also
- 9 References
- 10 External links









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Family: Kinesin (PF00225)









Summary

Domain organisation

Clans

Alignments

HMM logo

Trees

Curation & models

Species

Interactions

Structures

Jump to... 🐠



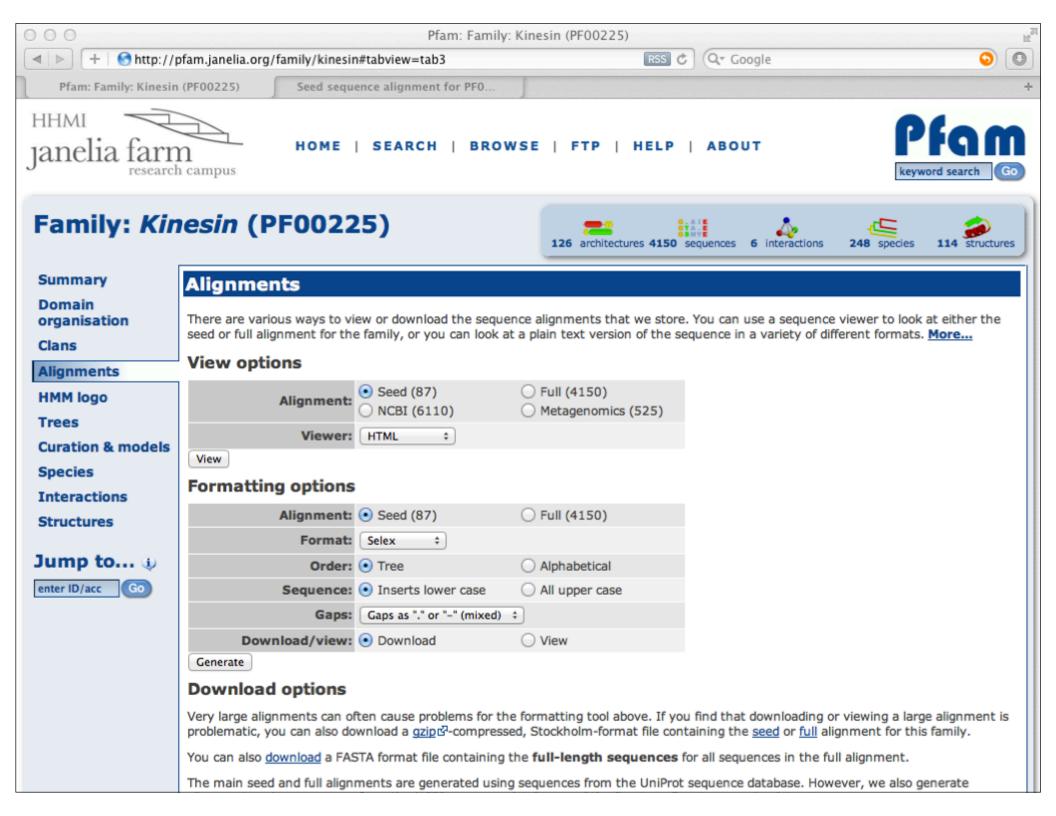


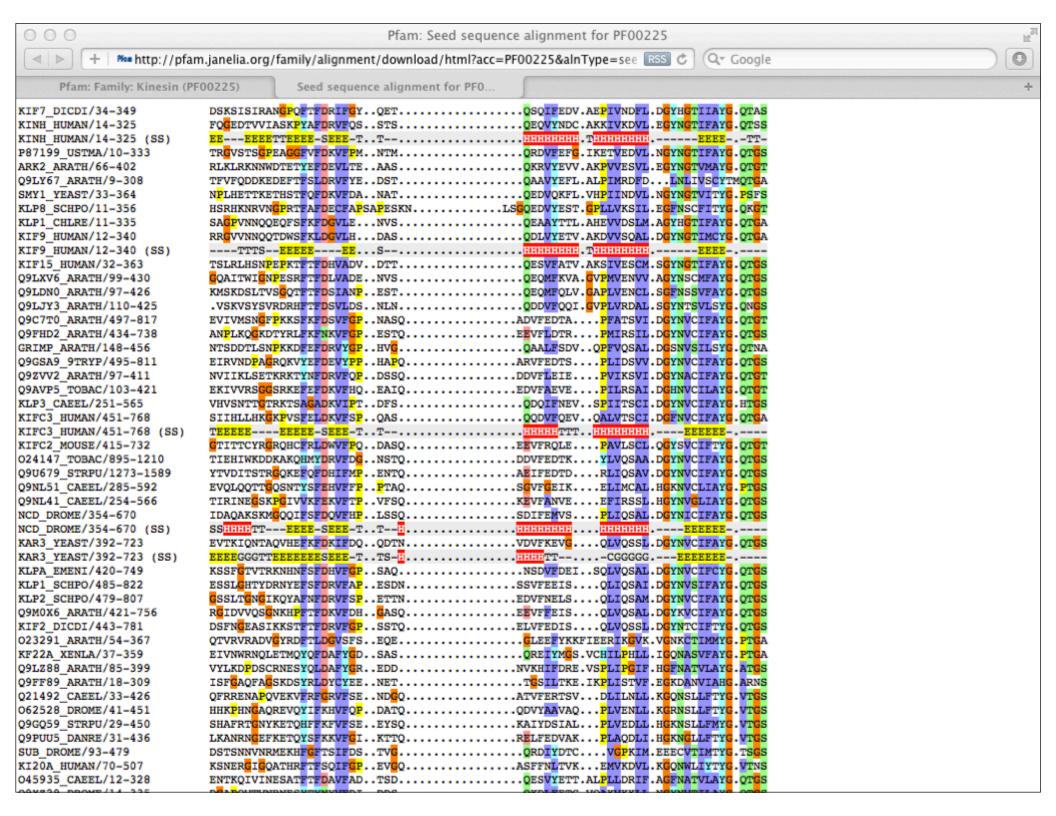
Pfam Clans

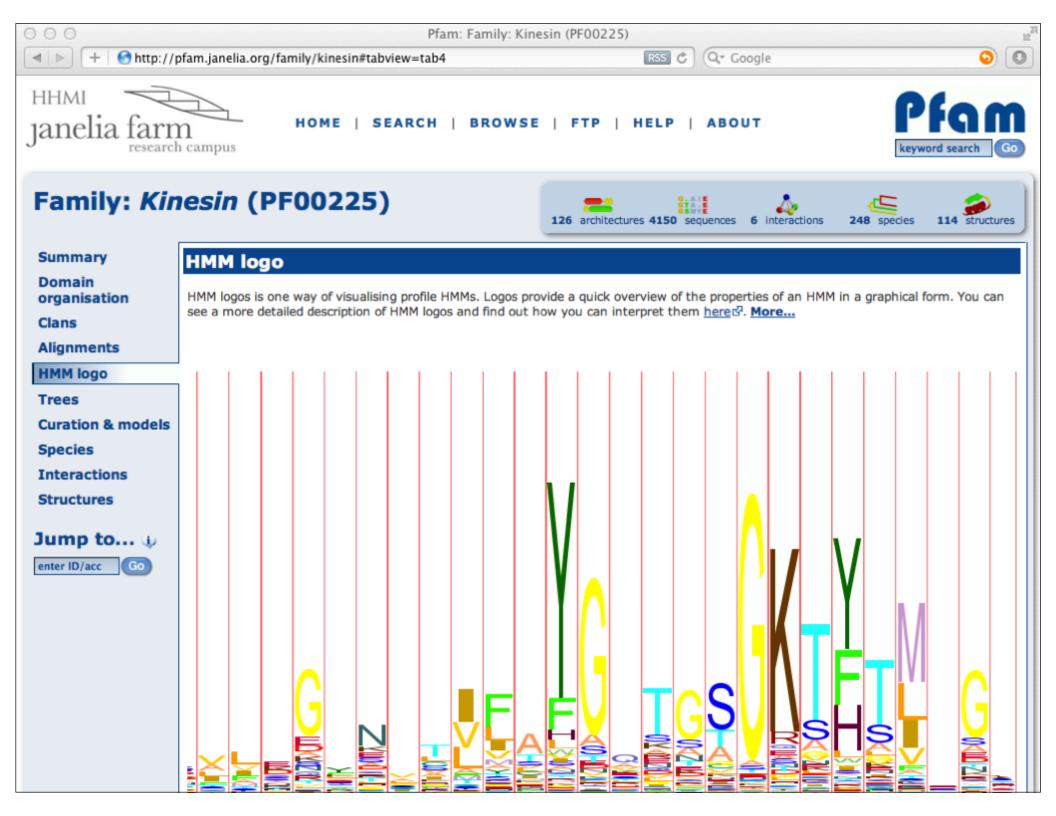
Zeta toxin

This family is a member of clan AAA (CL0023), which contains the following 157 members:

,			3	
6PF2K	AAA	AAA-ATPase like	AAA 10	AAA 2
AAA 3	AAA 5	AAA 6	<u>AAA 7</u>	AAA 8
AAA 9	AAA PrkA	ABC ATPase	ABC tran	ABC tran 2
Adeno IVa2	Adenylsucc synt	ADK	AFG1 ATPase	AIG1
APS kinase	Arch ATPase	<u>Arf</u>	<u>ArgK</u>	ArsA ATPase
ATP-synt ab	ATP bind 1	ATP bind 2	Bac DnaA	<u>CbiA</u>
<u>CoaE</u>	CobA CobO BtuR	CobU	<u>cobW</u>	<u>CPT</u>
CTP synth N	Cytidylate kin	DAP3	DEAD	DEAD 2
DLIC	DNA pack C	DNA pack N	DNA pol3 delta	DnaB C
<u>dNK</u>	DUF1253	DUF1611	DUF2075	DUF2478
DUF258	DUF2813	DUF463	DUF699	DUF815
DUF853	DUF87	DUF927	Dynamin N	Exonuc V gamma
FeoB N	Fer4 NifH	Flavi DEAD	FTHFS	FtsK SpoIIIE
G-alpha	Gal-3-0 sulfotr	GBP	GSPII E	GTP EFTU
Gtr1 RagA	Guanylate kin	GvpD	HDA2-3	Helicase C
Herpes Helicase	Herpes ori bp	Herpes TK	<u>IIGP</u>	<u>IPPT</u>
<u>IPT</u>	IstB IS21	<u>KaiC</u>	KAP NTPase	Kinesin
Kinesin-relat 1	Kinesin-related	KTI12	LpxK	<u>MCM</u>
Mg chelatase	MipZ	Miro	MMR HSR1	<u>MobB</u>
<u>MukB</u>	MutS V	Myosin head	NACHT	NB-ARC
NOG1	NTPase 1	ParA	Parvo NS1	PAXNEB
PduV-EutP	<u>PhoH</u>	PIF1	Podovirus Gp16	Polyoma Ig T C
Pox A32	PPK2	PPV E1 C	PRK	Rad17
Rad51	Ras	RecA	Rep fac C	ResIII
RHD3	RHSP	RNA12	RNA helicase	RuvB N
SecA DEAD	<u>Septin</u>	Sigma54 activat	<u>SKI</u>	SMC N
SNF2 N	Spore IV A	SRP54	SRPRB	Sulfotransfer 1
Sulfotransfer 2	Sulphotransf	T4SS-DNA transf	Terminase 1	Terminase 3
Terminase 6	Terminase GpA	Thymidylate kin	TIP49	<u>TK</u>
<u>TniB</u>	Torsin	TraG-D C	TrwB AAD bind	UPF0079
<u>UvrD-helicase</u>	Viral helicase1	VirC1	VirE	YhjQ







Pfam: Family: Kinesin (PF00225)









HOME | SEARCH | BROWSE | FTP | HELP | ABOUT

Family: Kinesin (PF00225)



Summary

Domain organisation

Clans

Alignments

HMM logo

Trees

Curation & models

Species

Interactions

Structures

Jump to... 🕦





Curation and family details

This section shows the detailed information about the Pfam family. You can see the definitions of many of the terms in this section in the glossary and a fuller explanation of the scoring system that we use in the scores section of the help pages.

Curation (1)

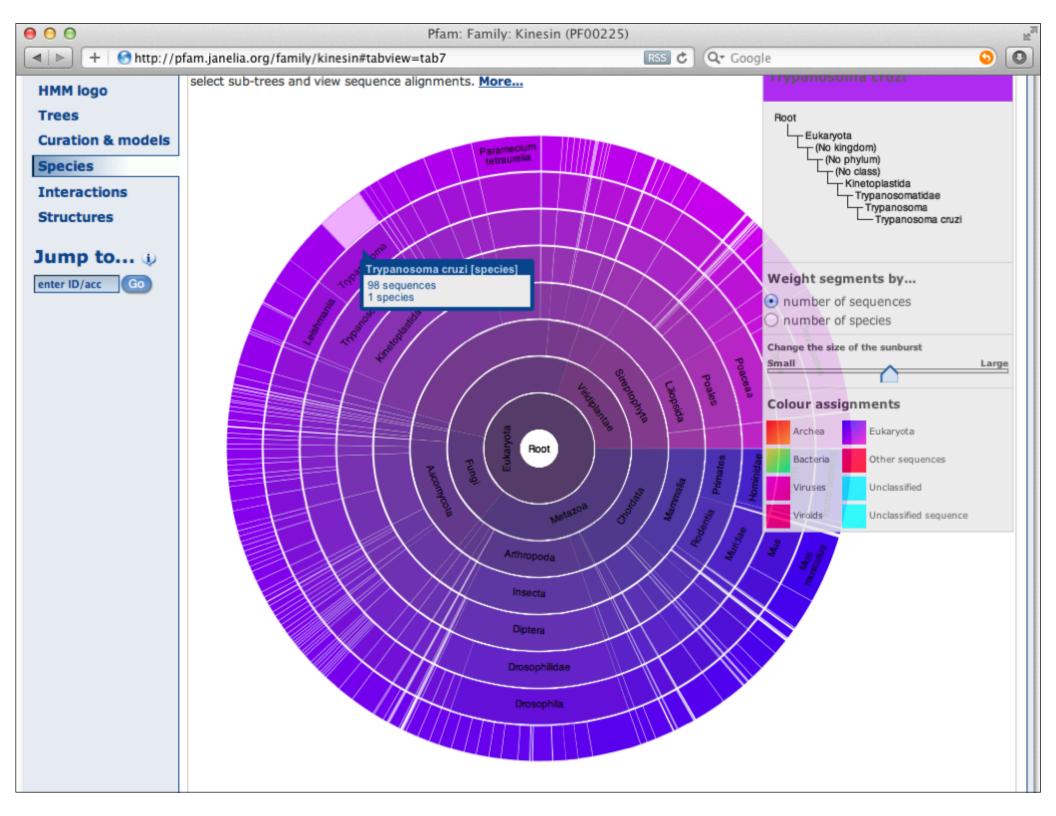
	Seed source:	Prosite
	Previous IDs:	kinesin;
	Type:	Domain
_	Author:	Bateman A, Finn RD
	Number in seed:	87
	Number in full:	4150
	Average length of the domain:	
	Average identity of full alignment:	
	Average coverage of the sequence by the domain:	

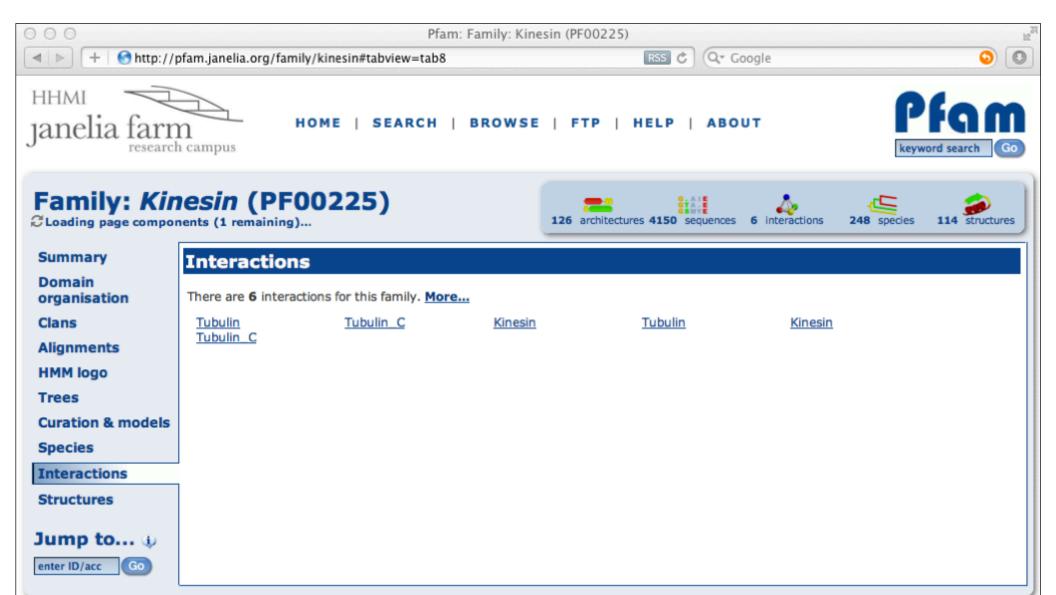
HMM information (1)

	build method: hmmbuild -o /dev/null HMM SEED search method: hmmsearch -Z 11384036 -E 1000cpu 4 HMM pfamseq			
Model details:	Parameter	Sequence	Domain	
	Gathering cut-off	22.5	22.5	

Gathering cut-off	22.5	22.5
Trusted cut-off	22.5	22.5
Noise cut-off	22.4	22.4

Model length: 333 Family (HMM) version: 17





Questions or comments: pfam@janelia.hhmi.org
Howard Hughes Medical Institute



HOME | SEARCH | BROWSE | FTP | HELP | ABOUT



Family: Kinesin (PF00225)



Summary

Domain organisation

Clans

Alignments

HMM logo

Trees

Curation & models

Species

Interactions

Structures

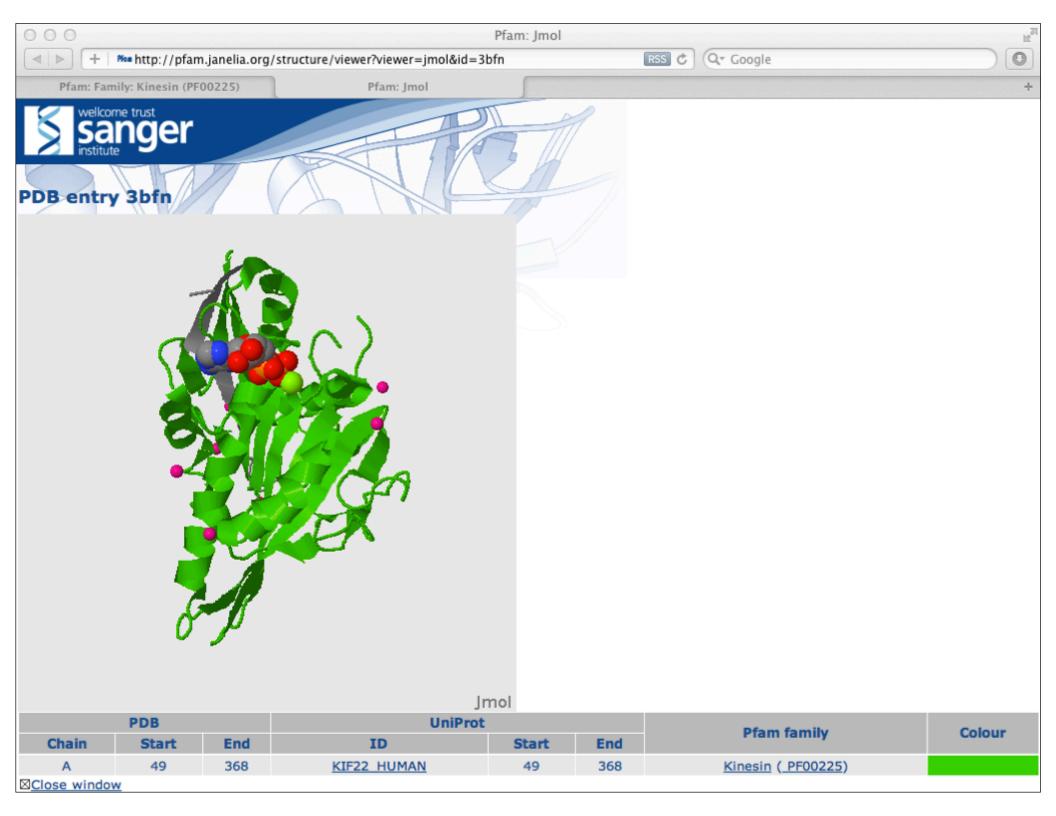
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For those sequences which have a structure in the <u>Protein DataBank</u>\$\overline{C}\$, we use the mapping between <u>UniProt</u>\$\overline{C}\$, PDB and Pfam coordinate systems from the <u>PDBe</u>\$\overline{C}\$ group, to allow us to map Pfam domains onto UniProt sequences and three-dimensional protein structures. The table below shows the structures on which the **Kinesin** domain has been found.

UniProt entry	UniProt residues	PDB ID	PDB chain ID	PDB residues	View
A8BKD1 GIALA	11 - 335	2,,,,	Α	11 - 335	Jmol AstexViewer SPICE ₽
		2vvg	В	11 - 335	<u>Jmol</u> <u>AstexViewer</u> <u>SPICE</u> ☐
CENPE HUMAN	12 - 329	145-	Α	12 - 329	<u>Jmol</u> <u>AstexViewer</u> <u>SPICE</u> ☐
		<u>1t5c</u>	В	12 - 329	Jmol AstexViewer SPICE ₽
KAR3 YEAST	392 - 723	<u>1f9t</u>	Α	392 - 723	Jmol AstexViewer SPICE ₽
		<u>1f9u</u>	Α	392 - 723	Jmol AstexViewer SPICE ₽
		<u>1f9v</u>	Α	392 - 723	Jmol AstexViewer SPICE &
		<u>1f9w</u>	Α	392 - 723	Jmol AstexViewer SPICE &
			В	392 - 723	Jmol AstexViewer SPICE ₽
		3kar	Α	392 - 723	Jmol AstexViewer SPICE ₽
	11 - 352		Α	11 - 352	Jmol AstexViewer SPICE ₽
KI13B HUMAN		3gbj	В	11 - 352	Jmol AstexViewer SPICE ₽
				C	11 - 352
		1::6	Α	24 - 359	Jmol AstexViewer SPICE ₽
		<u>1ii6</u>	В	24 - 359	Jmol AstexViewer SPICE ₽
		<u>1q0b</u>	Α	24 - 359	Jmol AstexViewer SPICE ₽
			В	24 - 359	Jmol AstexViewer SPICE 대
		1x88	Α	24 - 359	Jmol AstexViewer SPICE ₽
			В	24 - 359	Jmol AstexViewer SPICE ₽
			Α	24 - 359	Jmol AstexViewer SPICE 대





HMMER

biosequence analysis using profile hidden Markov models



Home Search

Results Software

Help

About



HMMER3: a new generation of sequence homology search software

HMMER is used for searching sequence databases for homologs of protein sequences, and for making protein sequence alignments. It implements methods using probabilistic models called profile hidden Markov models (profile HMMs).

Compared to BLAST, FASTA, and other sequence alignment and database search tools based on older scoring methodology, HMMER aims to be significantly more accurate and more able to detect remote homologs because of the strength of its underlying mathematical models. In the past, this strength came at significant computational expense, but in the new HMMER3 project, HMMER is now essentially as fast as BLAST.

As part of this evolution in the HMMER software, we are committed to making the software available to as many scientists as possible. Earlier releases of HMMER were restricted to command line use. To make the software more accessible to the wide scientific community, we now provide servers that allow sequence searches to be performed interactively via the Web.

The current version is HMMER 3.0 (28 March 2010) and can be downloaded from the software section of the site. Previous versions of the HMMER software can be obtained from the archive section.

If you have used the HMMER website, please consider citing the following reference that describes this work:

HMMER web server: interactive sequence similarity searching

☑ R.D. Finn, J. Clements, S.R. Eddy

Download HMMER

Get the latest version

v3.0

Release notes (28 March 2010)



Alternative Download Options Source

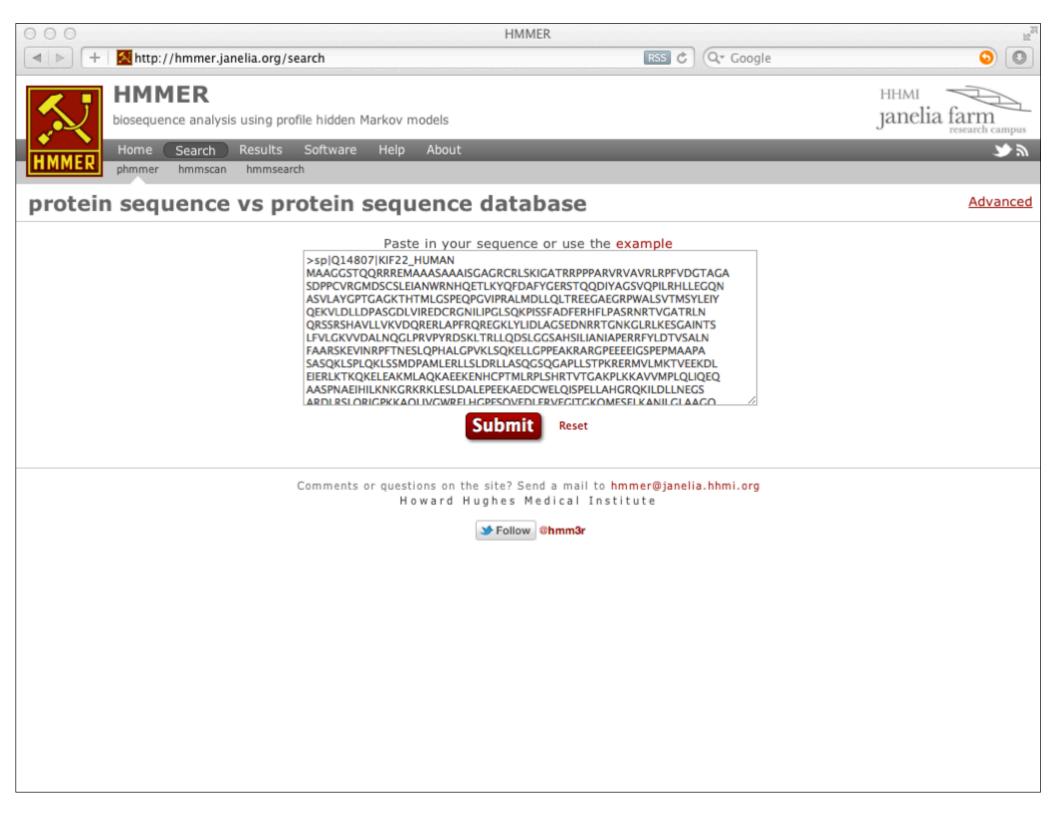
Search

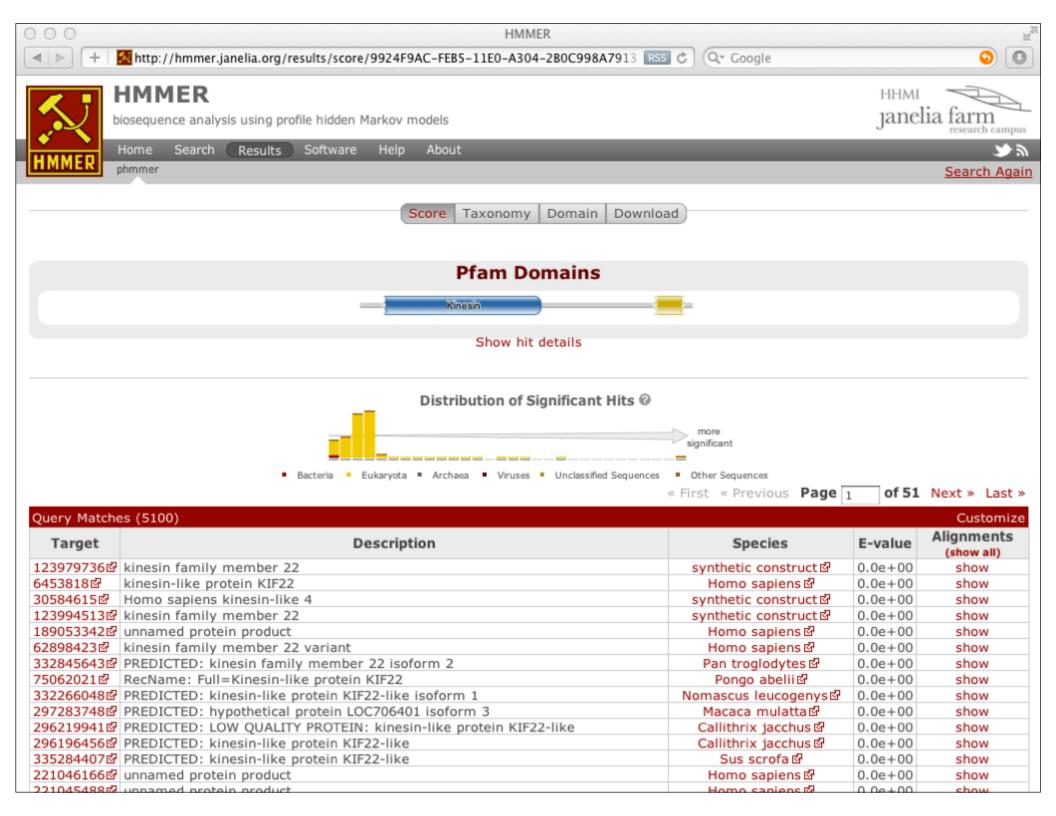
Perform an interactive search now.

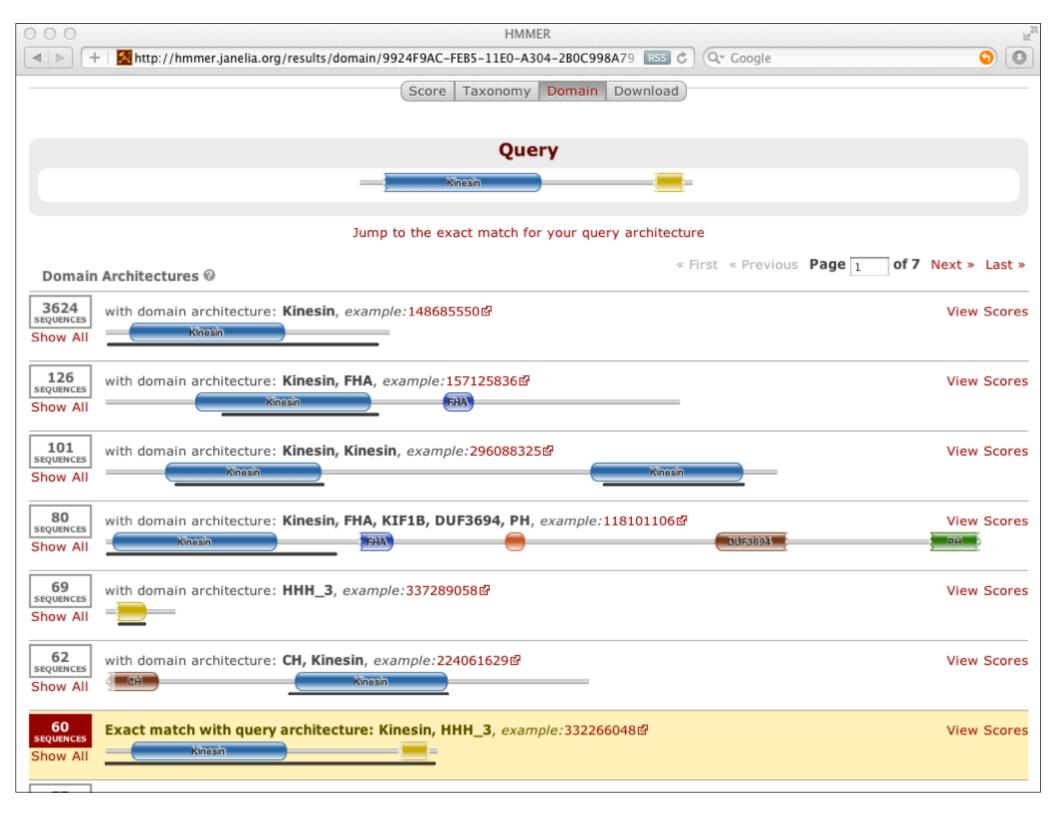
Search

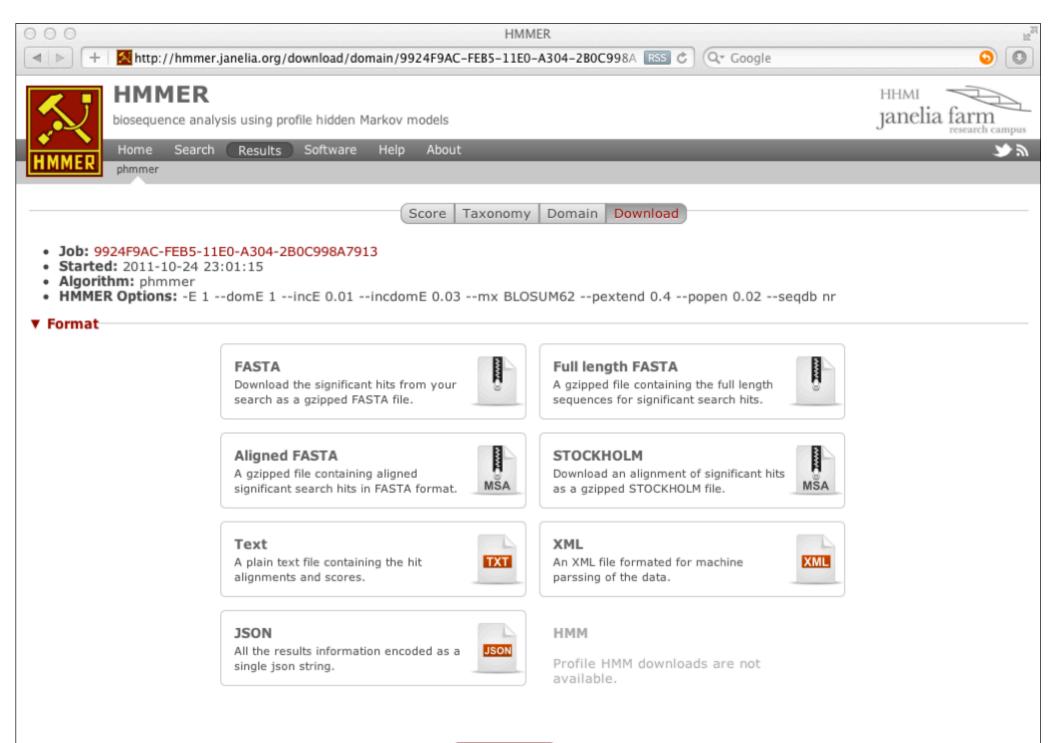
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Search SUPERFAMILY

Home

SEARCH

Keyword search

Sequence search

SUPERFAMILY Description

SUPERFAMILY is a database of structural and functional annotation for all proteins and genomes.

BROWSE

Organisms

--- Taxonomy

--- Statistics

SCOP

.... Hierarchy

Ontologies

.... GO

---- EC

TOOLS

.... Phenotype

Compare genomes

Phylogenetic trees

The SUPERFAMILY annotation is based on a collection of hidden Markov models, which represent structural protein domains at the SCOP superfamily level. A superfamily groups together domains which have an evolutionary relationship. The annotation is produced by scanning protein sequences from over 1,700 completely sequenced genomes against the hidden Markov models.

For each **protein** you can:

- Submit sequences for SCOP classification
- View domain organisation, sequence alignments and protein sequence details

For each **genome** you can:

- Examine superfamily assignments, phylogenetic trees, domain organisation lists and networks
- Check for over- and under-represented superfamilies within a genome

For each **superfamily** you can:

- Inspect SCOP classification, functional annotation, Gene Ontology annotation, InterPro abstract and genome assignments
- Explore taxonomic distribution of a superfamily across the tree of life

All annotation, models and the database dump are freely available for download to everyone. Description cont.

ABOUT

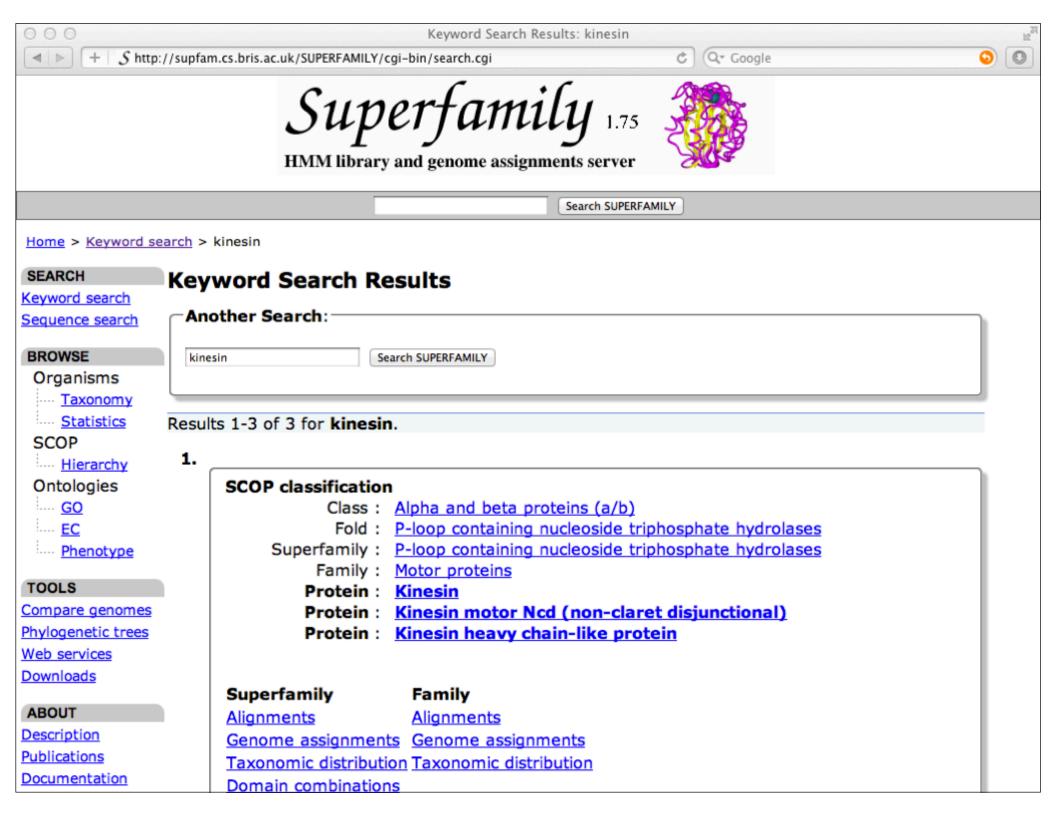
Description **Publications**

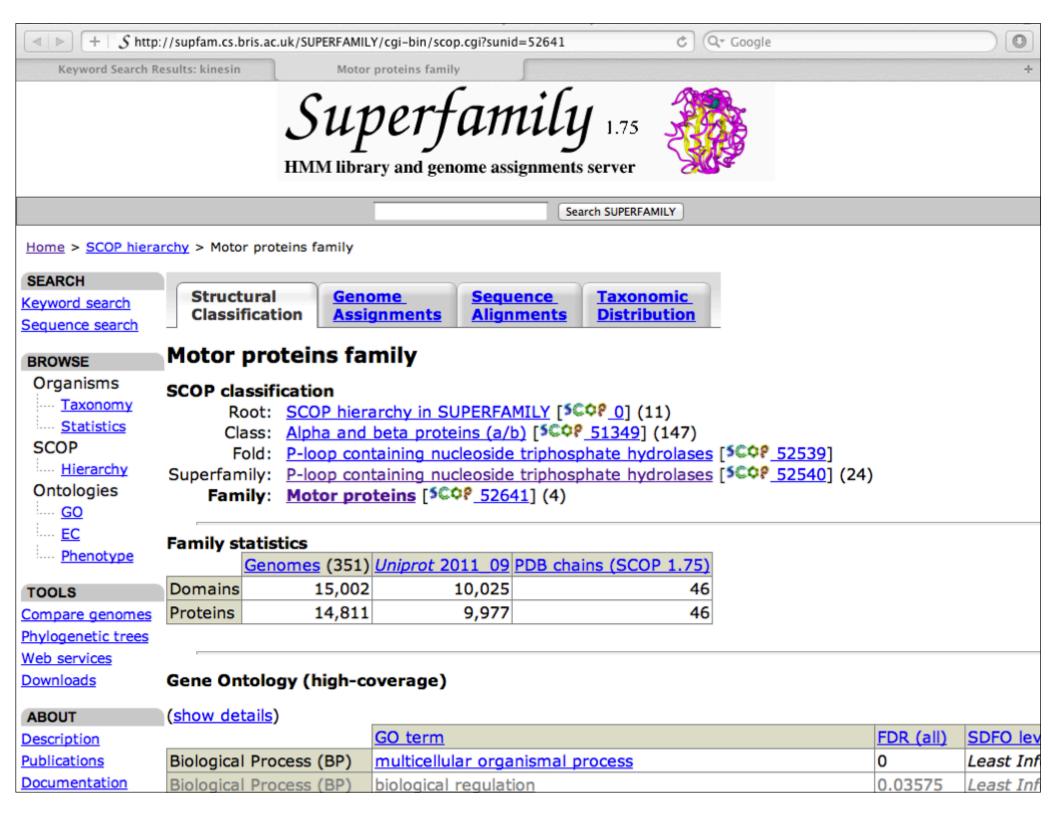
Documentation

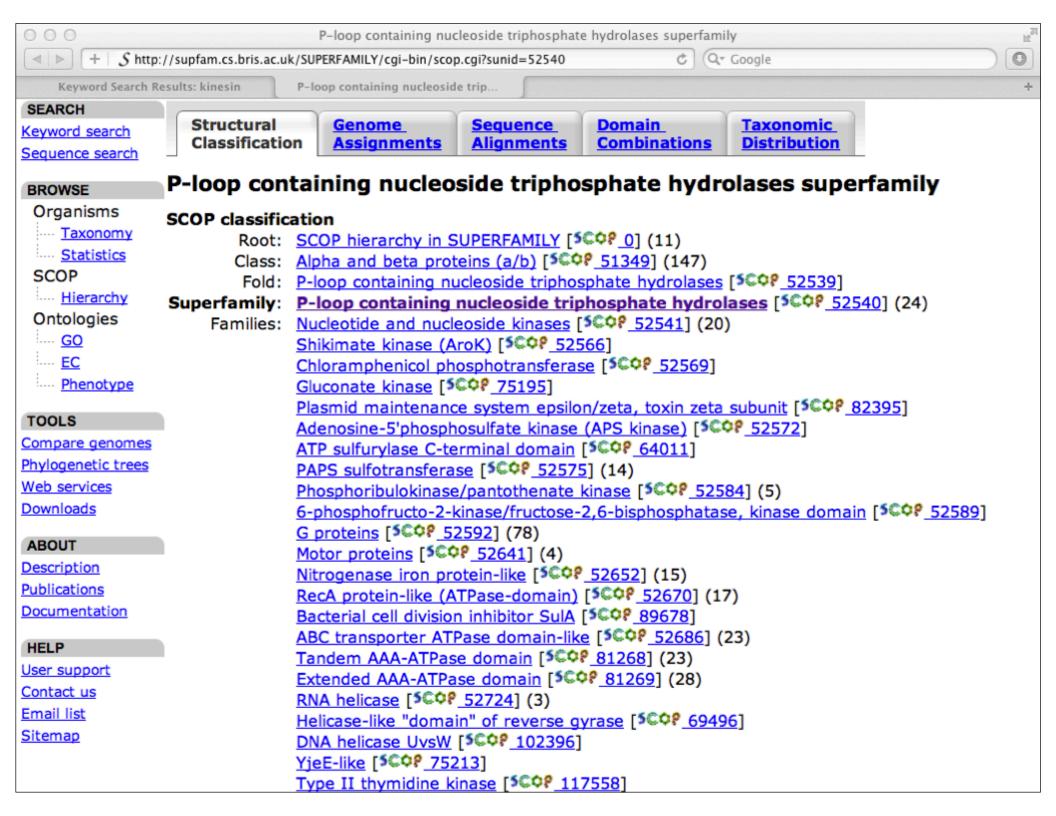
Web services Downloads

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Major Features









That's it!